SOUTH FLORIDA WATER MANAGEMENT DISTRICT

# South Miami-Dade Exploratory Statistical Analysis Report

# South Miami-Dade Water Issues Coordination Roundtable Discussion – March 1, 2011

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# Title of Report:

## South Miami-Dade Statistical Data Analyses

Prepared for: SFWMD Prepared by: Eric P. Smith

#### **Purpose:**

Develop a tool to provide insights into relationships among and between hydrologic and water quality data for the region



## This report is the 3<sup>rd</sup> part of a three-phase study

- 1. Compilation of Data
- 2. Data Scrub
- 3. Exploratory Analysis

# **Scope of Study**

Project Area is located:

- SE Miami-Dade County
- South of the C-4 canal
- East of the L31W levee
- Includes SFWMD water within Florida and Biscayne Bay



## **Source of Data for Statistical Analysis**

- SFWMD, USGS, DERM and Biscayne National Park databases
- Data was 'scrubbed' under a separate contract
  - Eliminate anomalous data points and
  - Fill in data gaps with estimated data where appropriate

Period of Record – 01/01/2000 through 12-31-2009

**Types of data analyzed**:

#### **Daily Timeseries**

Groundwater Levels (168 stations) Surface Water Stage (154 stations) Canal/Structure Flow (60 stations) Rainfall Gage Recorders (29 stations)

Discrete (random) and Continuous (15 minute interval) Water Quality (182 Salinity stations)

The report is a tool to aid in scientific investigation of data relationships and trends in the area.

It provides insights into relationships among and between hydrologic and water quality data for the region.

The report should not be considered an "Answer Machine"

Report includes the computation of data correlations to aid in understanding the relationships in the data

## A simple description or definition of Correlation Coefficients:

- A measure of the relationship between two variables
- Correlation coefficients are useful because they can indicate a predictive relationship in data sets

## **Types of Correlations calculated for this Report:**

- Pearson:
  - Traditional Correlation Good for Linear and Normal Distributions
- Spearman:
  - A Rank Correlation and doesn't require a normal distribution Not as sensitive to odd observations or outliers
- Kendall:

Also a Rank or Order based Correlation Good for monotonic relationships between series

Rank Correlations:

Ranks are computed and correlations between the ranks are calculated

#### **Examples plots of Pearson's Correlation Coefficients**



The correlation coefficients (Pearson's) reflect the noisiness and direction of a linear relationship. Not slope or non-linear variation.

#### **Pearson's Correlation Coefficient and Linearity**

- 1. Pearson's is good with a normal or linear distribution
- 2. Not distributed normally and not linear
- Distribution is linear, but has a different regression line one outlier changes the regression.
- 4. One outlier is enough to produce a high correlation



Each graph shows the same basic statistics: Mean (.75), Variance (4.12), Correlation (0.816), and Regression Line (y = 3 + 0.5x)

#### **Analyses Included in the Report:**

Correlation for stations with (Stage, Groundwater, Rain, Flow, Salinity) •Same data type •Different types •Full period of record for the study •Wet season & dry season

Lag correlations

No lag, and 1 to 5 days. (i.e.: Lag 1 is the previous day) between variables of the same type or different types

Neighboring station relationships Correlations by station and type for each station with the six closest in distance

## **Principal Components Analysis(PCA)/Factor Analysis**

Helps summarize data and relationships between variables.

#### Scree plots :

Shows eigenvalues vs. eigenvectors or number of factors

#### Variance Explained plot:

Displays the proportion of total variance for each component and the cumulative proportion of the variance explained.

The PCA use the number of factors with eigenvalues above 1 .(Look for the elbow)



#### Principal Components Analysis(PCA)/Factor Analysis

Shows the sets of variables identified by the rotated factor pattern of rain data.

Variables with similar values grouped or flagged with a star

Rotated Factor Pattern													
	Factor1		Factor2		Factor3								
S20G_Rain	77	*	27		23								
S20F_Rain	77	*	28		22								
S179_Rain	76	*	30		24								
S21A_Rain	75	*	26		20								
S21_Rain	72	*	35		24								
S20_Rain	71	*	23		22								
HOMESFS_rain	71	*	35		26								
S165_Rain	71	*	40		21								
S167_Rain	70	*	38		24								
S18C_Rain	69	*	29		18								
S177_Rain	67	*	38		17								
MDTS_rain	67	*	18		15								
tpts_rain	67	*	14		16								
S332_Rain	63	*	38		19								
S174_Rain	62	*	45		21								
JBTS_rain	62	*	21		17								
S123_rain	61	*	39		23								
S334_rain	29		88	*	20								
S335_rain	29		88	*	20								
S336_Rain	36		83	*	21								
S338_Rain	48	*	65	*	22								
S331W_rain	53	*	62	*	23								
S331_Rain	48	*	60	*	22								
S26_rain	47		48	*	28								
miamai_ap_rain	22		21		82	*							
TAMI_AIR_rain	22		19		82	*							
PERRINE_Rain	27		22		81	*							
miami_2_Rain	25		15		77	*							
Printed values are	multiplie	ed l	by 100 an	d r	ounded to	D							
the nearest intege	er. Values	s gr	eater tha	ın (	0.474122								
are flagged by an	'*'.												

# Principal Components Analysis(PCA)/Factor Analysis

- Bi-plots summarizes sites and times in one display
- Useful to identify sites with similar and extreme measurement patterns

Note: 2064 represents one day when rain was considerably greater than other times



## **Correlation Matrix for Rain Stations**

ų.	rain_Sp	earmai	n1.csv																												-
	A	в	C	D	E	F	G	н		J	К	L	M	N	0	P	Q	B	S	T	U	V	V	X	Y	Z	AA	AB	AC	AD	AE
1	_TYPE	_NAME_H	HOMES	JBTS_ra	MBTS_rain	MDTS_rain	PERRINE_R	S123_rain	S165_Rain	S167_Rain	S174_Raii :	S177_Raii	S179_Rair	S18C_Rair	S20F_Rai	S20G_Ra	S20_Rai	S21A_R-	S21_Raii \$	526_rair	S331W_r 3	S331_Ra	S332_R. :	S334_ra 🛛	S335_ra	S336_R.	S338_R-1	TAMLA I	miamai_ i	miami_2	tpts_rain
2	MEAN	- 1	0.1405	0.0843	0.0982337	0.1077018	0.161922296	0.1186329	0.135207	0.135413	0.13992	0.12385	0.144065	0.164078	0.120631	0.12724	0.1272	0.1184	0.1097	0.1551	0.1568	0.1249	0.1309	0.1667	0.1667	0.136	0.132	0.1429	0.173	0.1426	0.1187
3	STD		0.4932	0.3518	0.389512	0.4264105	0.483622783	0.4228182	0.451254	0.436866	0.42764	0.41217	0.510214	0.537026	0.391404	0.42663	0.4579	0.4116	0.3864	0.471	0.4967	0.4132	0.4059	0.5079	0.5079	0.41	0.4059	0.4458	0.5119	0.4443	0.4353
4	N		3433	3489	1703	3481	3449	3577	3634	3640	3563	3645	3488	3627	3646	3634	2818	3609	3623	3624	3626	3069	3627	3596	3596	3607	3599	3583	3640	3493	3342
5	CORR	HOMES	1	0.4952	0.5155851	0.5142516	0.472795454	0.5956339	0.698253	0.759515	0.64944	0.65154	0.776439	0.610345	0.66724	0.66852	0.6042	0.6382	0.6534	0.5532	0.6415	0.5796	0.6256	0.554	0.554	0.5901	0.6058	0.4344	0.4324	0.4127	0.4984
6	CORR	JBTS_ra	0.4952	1	0.5948848	0.5402961	0.351353638	0.4419052	0.510973	0.494179	0.46559	0.50705	0.492068	0.531616	0.507468	0.52379	0.5212	0.4856	0.5036	0.4514	0.4719	0.4441	0.4987	0.4339	0.4339	0.4574	0.4678	0.3068	0.3221	0.341	0.5082
7	CORR	MBTS_(	0.5156	0.5949	1	0.6590065	0.348704523	0.4781809	0.486895	0.525464	0.46053	0.50358	0.534498	0.550152	0.525991	0.51972	0.5611	0.5309	0.5272	0.4527	0.4758	0.418	0.477	0.4452	0.4452	0.4748	0.4702	0.3186	0.3448	0.3438	0.637
8	CORR	MDTS_(	0.5143	0.5403	0.6590065	1	0.341202415	0.4697776	0.5036	0.521892	0.48725	0.50524	0.518806	0.529319	0.545038	0.52818	0.5988	0.4958	0.5111	0.4458	0.4676	0.4495	0.468	0.442	0.442	0.4602	0.4621	0.2987	0.3159	0.3424	0.6004
9	CORR	PERRIN	0.4728	0.3514	0.3487045	0.3412024	1	0.4251644	0.459387	0.462827	0.43562	0.40406	0.456237	0.405552	0.444993	0.4596	0.4158	0.4089	0.459	0.4203	0.4805	0.4661	0.4201	0.4265	0.4265	0.4301	0.4495	0.7407	0.6801	0.6109	0.333
10	CORR	S123_rai	0.5956	0.4419	0.4781809	0.4697776	0.425164446	1	0.662384	0.612094	0.56341	0.54447	0.617076	0.514744	0.631672	0.63671	0.556	0.6223	0.6885	0.5736	0.6086	0.5598	0.5115	0.5473	0.5473	0.5746	0.5975	0.3878	0.4015	0.3833	0.4538
11	CORR	S165_Ra	0.6983	0.511	0.4868949	0.5036004	0.459386797	0.6623839	1	0.723902	0.63889	0.61408	0.722959	0.580738	0.688517	0.70833	0.5842	0.6985	0.7315	0.5732	0.6614	0.6328	0.5939	0.5728	0.5728	0.6116	0.6408	0.4012	0.402	0.3815	0.4853
12	CORR	S167_Ra	0.7595	0.4942	0.5254644	0.521892	0.462826842	0.6120938	0.723902	1	0.68252	0.64782	0.743127	0.608217	0.678717	0.66904	0.591	0.6341	0.6686	0.5498	0.6634	0.6271	0.6195	0.5712	0.5712	0.5977	0.6227	0.4328	0.4239	0.412	0.4998
13	CORR	S174_Ra	0.6494	0.4656	0.4605303	0.4872488	0.435620698	0.563411	0.638885	0.682519	1	0.69319	0.642427	0.592347	0.616061	0.60667	0.5645	0.5715	0.6071	0.5176	0.6601	0.6198	0.6814	0.5708	0.5708	0.6058	0.6429	0.4121	0.4045	0.3698	0.476
14	CORR	S177_Ra	0.6515	0.507	0.5035758	0.5052358	0.404061016	0.5444696	0.614081	0.647817	0.69319	1	0.650428	0.649727	0.598398	0.59935	0.5674	0.5701	0.5928	0.5234	0.6186	0.5783	0.7404	0.5395	0.5395	0.572	0.5907	0.3778	0.3706	0.3595	0.493
15	CORR	S179_Ra	0.7764	0.4921	0.5344975	0.5188059	0.456236857	0.6170764	0.722959	0.743127	0.64243	0.65043	1	0.603669	0.740855	0.73311	0.6242	0.6931	0.7019	0.5676	0.6501	0.5859	0.6086	0.5349	0.5349	0.579	0.6028	0.4258	0.4299	0.4193	0.5238
16	CORR	S18C_R	0.6103	0.5316	0.5501522	0.529319	0.405551633	0.5147439	0.580738	0.608217	0.59235	0.64973	0.603669	1	0.58745	0.58725	0.5998	0.5577	0.5675	0.5029	0.5842	0.5327	0.6267	0.4904	0.4904	0.5121	0.5511	0.3639	0.3595	0.3508	0.5056
17	CORR	S20F_R	0.6672	0.5075	0.5259911	0.5450381	0.444993188	0.6316716	0.688517	0.678717	0.61606	0.5984	0.740855	0.58745	1	0.80299	0.635	0.7083	0.7031	0.5512	0.6166	0.5505	0.5645	0.5341	0.5341	0.5661	0.5892	0.3882	0.4106	0.4049	0.5239
18	CORR	S20G_R	0.6685	0.5238	0.5197176	0.5281755	0.459602094	0.6367124	0.708332	0.669045	0.60667	0.59935	0.733112	0.587255	0.80299	1	0.6123	0.7364	0.7288	0.5624	0.6072	0.5543	0.5713	0.5302	0.5302	0.5616	0.587	0.3972	0.4194	0.4099	0.5185
19	CORR	S20_Rai	0.6042	0.5212	0.5610792	0.5988178	0.415811102	0.5559656	0.584189	0.591015	0.56449	0.56744	0.624211	0.599821	0.634989	0.61226	1	0.5646	0.6159	0.4934	0.5703	0.5486	0.5186	0.479	0.479	0.5081	0.5282	0.3909	0.3685	0.3795	0.5639
20	CORR	S21A_R	0.6382	0.4856	0.530862	0.4958469	0.408934158	0.6222819	0.698492	0.634077	0.57151	0.57005	0.693117	0.55773	0.708344	0.73643	0.5646	1	0.7538	0.5244	0.5909	0.5357	0.5504	0.4972	0.4972	0.5408	0.5681	0.3766	0.3844	0.3774	0.5148
21	CORR	S21_Rait	0.6534	0.5036	0.5271751	0.5111433	0.458984481	0.6885454	0.731488	0.668636	0.6071	0.59278	0.701942	0.56751	0.703095	0.72881	0.6159	0.7538	1	0.5818	0.6352	0.5945	0.562	0.5544	0.5544	0.6015	0.6286	0.4153	0.4146	0.4158	0.5119
22	CORR	S26_rair	0.5532	0.4514	0.4526818	0.4457968	0.420312403	0.5736029	0.573151	0.549833	0.51759	0.52341	0.56761	0.502893	0.551163	0.56238	0.4934	0.5244	0.5818	1	0.5722	0.5368	0.4991	0.5838	0.5838	0.6025	0.5679	0.3958	0.4505	0.4064	0.4277
23	CORR	S331V_r	0.6415	0.4719	0.4757696	0.4676039	0.480519408	0.608621	0.661371	0.663398	0.66006	0.6186	0.650146	0.584245	0.616553	0.60721	0.5703	0.5909	0.6352	0.5722	1	0.842	0.605	0.651	0.651	0.6924	0.7582	0.4277	0.4284	0.393	0.4617
24	CORR	S331_Ra	0.5796	0.4441	0.4179612	0.4494549	0.46612414	0.5598084	0.632837	0.627057	0.61982	0.57835	0.585894	0.532748	0.550475	0.55434	0.5486	0.5357	0.5945	0.5368	0.842	1	0.5612	0.6023	0.6023	0.635	0.707	0.4046	0.4028	0.3636	0.4138
25	CORR	S332_R	0.6256	0.4987	0.4769923	0.4680012	0.420120249	0.5114922	0.593863	0.619549	0.6814	0.74037	0.608557	0.626745	0.564524	0.57133	0.5186	0.5504	0.562	0.4991	0.605	0.5612	1	0.5231	0.5231	0.5539	0.5744	0.3783	0.3749	0.3588	0.4541
26	CORR	S334_ra	0.554	0.4339	0.4452035	0.4419738	0.426462491	0.5472944	0.57285	0.571153	0.57079	0.53952	0.534898	0.490382	0.534085	0.5302	0.479	0.4972	0.5544	0.5838	0.651	0.6023	0.5231	1	1	0.8857	0.667	0.392	0.41	0.3854	0.4065
27	CORR	S335_ra	0.554	0.4339	0.4452035	0.4419738	0.426462491	0.5472944	0.57285	0.571153	0.57079	0.53952	0.534898	0.490382	0.534085	0.5302	0.479	0.4972	0.5544	0.5838	0.651	0.6023	0.5231	1	1	0.8857	0.667	0.392	0.41	0.3854	0.4065
28	CORR	S336_R	0.5901	0.4574	0.4747532	0.4602189	0.430122734	0.5745693	0.611555	0.597683	0.60581	0.57198	0.578991	0.512053	0.566149	0.56158	0.5081	0.5408	0.6015	0.6025	0.6924	0.635	0.5539	0.8857	0.8857	1	0.7158	0.4117	0.4229	0.3927	0.451
29	CORR	S338_R	0.6058	0.4678	0.470239	0.4621309	0.449520524	0.5975113	0.64078	0.622736	0.64289	0.5907	0.60282	0.551144	0.589209	0.58703	0.5282	0.5681	0.6286	0.5679	0.7582	0.707	0.5744	0.667	0.667	0.7158	1	0.4172	0.4206	0.3802	0.4405
30	CURR	TAME A	0.4344	0.3068	0.3185665	0.2987128	0.740691909	0.3878131	0.401229	0.432759	0.41211	0.37783	0.425791	0.363944	0.388228	0.3972	0.3909	0.3766	0.4153	0.3958	0.4277	0.4046	0.3783	0.392	0.392	0.4117	0.4172	1	0.665	0.5765	0.314
31	CORR	miamai_	0.4324	0.3221	0.3448314	0.3158806	0.68014704	0.4015208	0.402024	0.423899	0.40448	0.37062	0.429918	0.359505	0.410642	0.41939	0.3685	0.3844	0.4146	0.4505	0.4284	0.4028	0.3749	0.41	0.41	0.4229	0.4206	0.665	1	0.663	0.3041
32	CORR	miami_2	0.4127	0.341	0.3438269	0.3424447	0.610943855	0.3833046	0.381524	0.411993	0.36982	0.35947	0.419268	0.35085	0.404864	0.40993	0.3795	0.3774	0.4158	0.4064	0.393	0.3636	0.3588	0.3854	0.3854	0.3927	0.3802	0.5765	0.663	1	0.3256
33	CURR	tpts_rain	0.4984	0.5082	0.6370066	0.6003568	0.332954189	0.4537865	0.485298	0.499804	0.47603	0.49304	0.523761	0.505578	0.523907	0.51852	0.5639	0.5148	0.5119	0.4277	0.4617	0.4138	0.4541	0.4065	0.4065	0.451	0.4405	0.314	0.3041	0.3256	1

#### **Heat Maps**

Help summarize relationships of data by representing the size correlations in groups of colors on and off the matrix diagonal

Values of high correlation on the diagonal are comparing the same variables

High values off the diagonal are variables to look at



#### **Regression Models** (stepwise regression procedure)

DEPVAR: dependent variable RMSE: square root of the mean square root

ReasN 3500A.csv

Intercept: gives the value of the intercept in the model

IN: Indepentent variablesP: number of parametersEDF: Degrees of freedomRSQ: R-squared of the model

	-														
	A	В	С	D	E	F	G	H	Т	U	Y	CZ	DA	DB	DC
1	_DEPVAR	_RMSE_	Intercept	MDTS_S	S175_H_	S175_T_	S177_H_	S177_T_	SWEVER1_	ANGEL_W	S178_C_Flow	_IN_	_P_	_EDF_	_RSQ_
2	MBTS_Stage_J	0.03734	2.174185									5	6	3636	0.992055
3	s179_T_Stage_D	0.03476	0.027827									5	6	3636	0.986365
4	S175_H_Stage_J	0.047687	-0.03538		-1	0.06373						5	6	3636	0.99827
5	S175_T_Stage_J	0.096894	-0.07807		0.20697	-1		0.5313				5	6	3636	0.97294
6	S177_H_Stage_J	0.152644	0.014628		0.25106		-1					5	6	3636	0.91181
7	S177_T_Stage_J	0.064273	0.017561		-0.0331			-1				5	6	3636	0.979658
19	SWEVER1_Stage_J	0.103752	-0.08663	0.1204	-0.0707				-1			5	6	3636	0.912485
20	ANGEL_WELL_km	0.248584	0.023645		0.31699					-1		5	6	3636	0.935607
26	S178_C_Flow_SK	11.56409	7.990156								-1	5	6	3636	0.869254
27	S178_S_Flow_SK	7.181994	-1.78172								0.572281882	5	6	3636	0.87408
28	S20G_S_Flow_SK	32.52369	-43.158	22.129								5	6	3636	0.604927
29	S25_C_Flow_SKRE	15.27393	15.18167									5	6	3636	0.494211
30	_3B_SE_B_Stage_C	0.183141	-0.71708									5	6	3636	0.964557
31	G334_H_Stage_D	0.238433	3.340191									5	6	3636	0.761829
32	G334_T_Stage_D	0.04544	0.005767									5	6	3636	0.99415
33	G93 H Stage D	0.184288	-0.01013							0.101852		5	6	3636	0.755543

#### Example analysis: S20F flow and salinity

- Illustrates how the report can be used to explore data relationships
- Important factors to consider when interpreting the data relationships
- The example shows some of the complications the analysis of a simple question may need to provide a very general answer.

"Does flow out of S20F cause changes in salinity, stage and water levels nearby?"

# Map of some of the stations for the Example Analysis:

Flow:S20F\_S, S21A\_S, S179\_SWell:BBCW6 (BBCW6GW1, BBCW6GW2), G3356Stage:S20F\_H, S21A\_H, S179\_HSalinity:BISC 124, BISC 123, BISC 122, BISC113, BISC16BOT,<br/>BISC24BOT, BISC34BOT, BISC14BOT, BISC32BOT,<br/>BISC22BOT, BISC129, BISC104



#### **Answer:**

- The analysis suggests there is a relationship between flow at S20F and salinity levels at nearby stations
- The relationship is strongest at the stations closer to S20F
- However the strength of the relationship is difficult to assess as there may be other factors involved
- This is suggested by the fact that salinity at stations farther from S20F are also correlated with flow at S20F, although the correlation is weaker





# **Questions?**

Links to Information and Data:

SFWMD Web site: Link to Miami-Dade Service Center Page

Map-based Interface to South Miami-Dade Water Issues Documents and Data

