



Lecture 14: Calibrating a RSM Sub-Regional Model Using PEST

This lecture introduces the Parameter Estimation (PEST) Software.

For more detailed information, refer to the PEST User Manual, PEST: Model-Independent Parameter Estimation. User Manual 5th Edition. Doherty, John. Watermark Numerical Computing. July, 2004.



NOTE:

A copy of the PEST User Manual can be found in the `$RSM/labs/lab13_PEST` directory.

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Palm Beach PEST Calibration - Setup

RSM

- Automated Parameter Estimation software (PEST) given the
 - Complexities of the model
 - Large number of model parameters
 - Observation data involved
- PEST analysis was conducted by creating parameter zones for
 - Aquifer conductivity
 - Canal network leakance
 - Canal network Manning's n
 - Lumped leakance for WCD canals
 - Levee seepage coefficients
 - Conductance for the tidal boundaries

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The automated Parameter Estimation approach was adopted because of the complexity of calibrating the RSM with a large number of model parameters that should be calibrated and the large number (>300) of observed time series that could be used for calibration. To simplify the parameter calibration, the parameters were lumped into spatial "zones" which received the same calibrated parameter value. This is consistent with the uncertainty associated with available parameter estimations. An objective function was created that summed the bias and root mean square error (RMSE) at each flow and stage calibration location.

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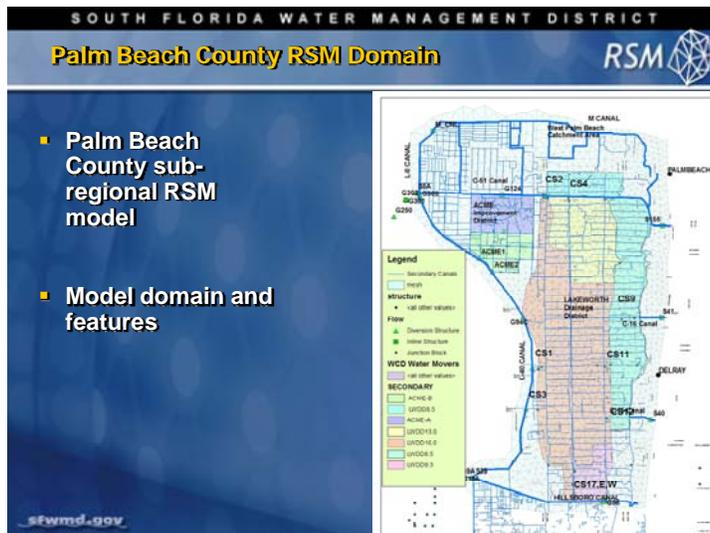
Palm Beach RSM v1.0 Calibration

RSM

- Objective was to minimize the weighted sum of squares of the bias and RMSE calculated at each observation point.
- For groundwater levels or surface water stages at a given site the calibration was considered to be satisfactory if either absolute criterion (within ± 1.0 foot) or the relative criterion (at least within the level of accuracy that the SFWMM was validated) was met.
- For flows, the criterion was that the measured and computed monthly flow volumes need to be of the same direction and order of magnitude.

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The files used in this lecture can be found in the Palm Beach directory (\$RSM/data/palmbeach). These files are included for browsing because it is likely that the student will need to review these files during the lecture. The PEST manual is also a useful document.



- Palm Beach County sub-regional RSM model
- Model domain and features

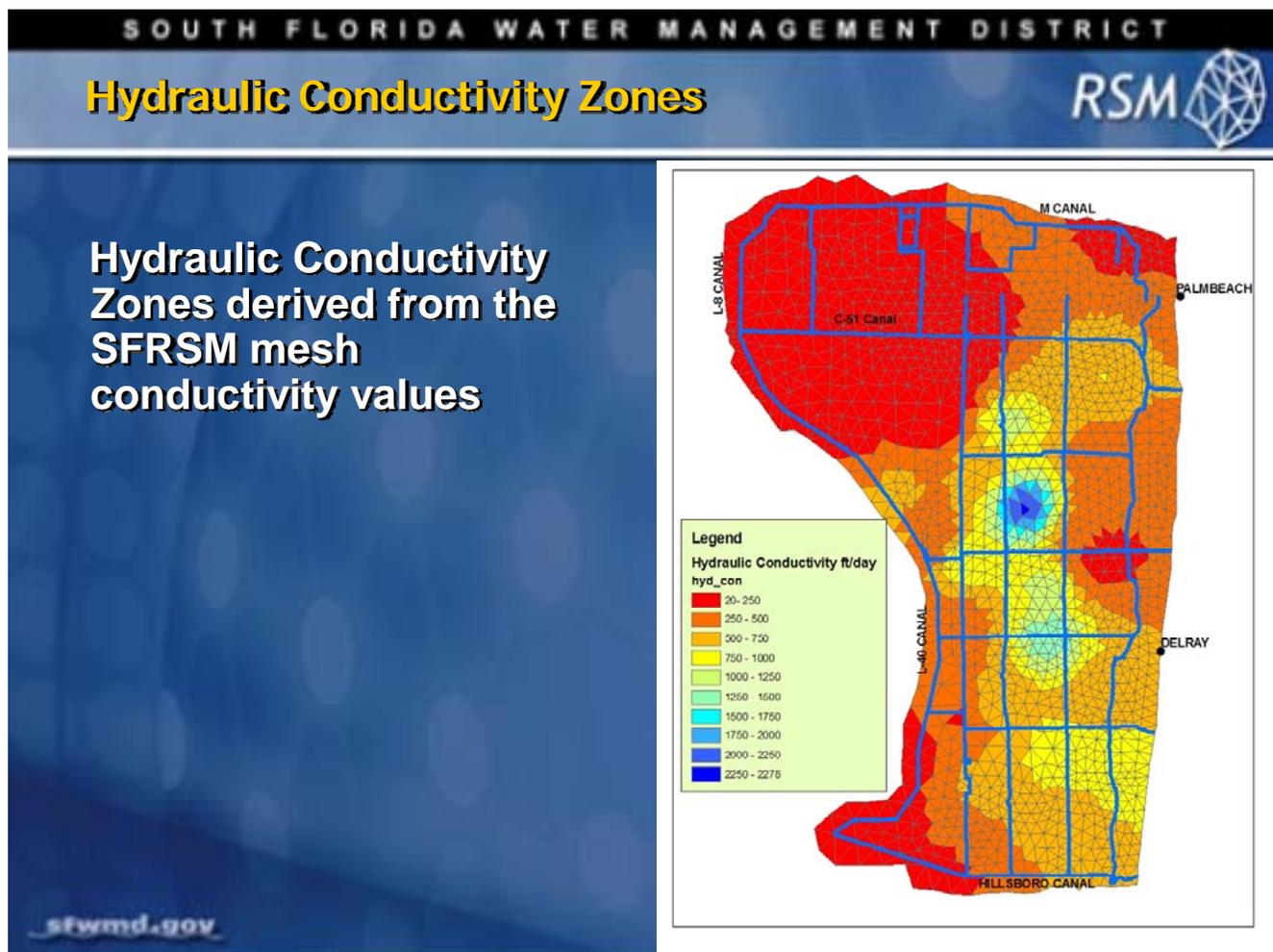
The surface water management practices in Palm Beach County are complex, with both primary and secondary canals and Water Control Districts (WCDs) with maintained water levels. The primary and secondary systems provide both drainage and water supply to the areas they serve. The “maintained” systems are subject to water level fluctuations depending on the flood control or water supply functions they are providing at any given time.

The primary canals in the model area include Hillsboro canal along the southern

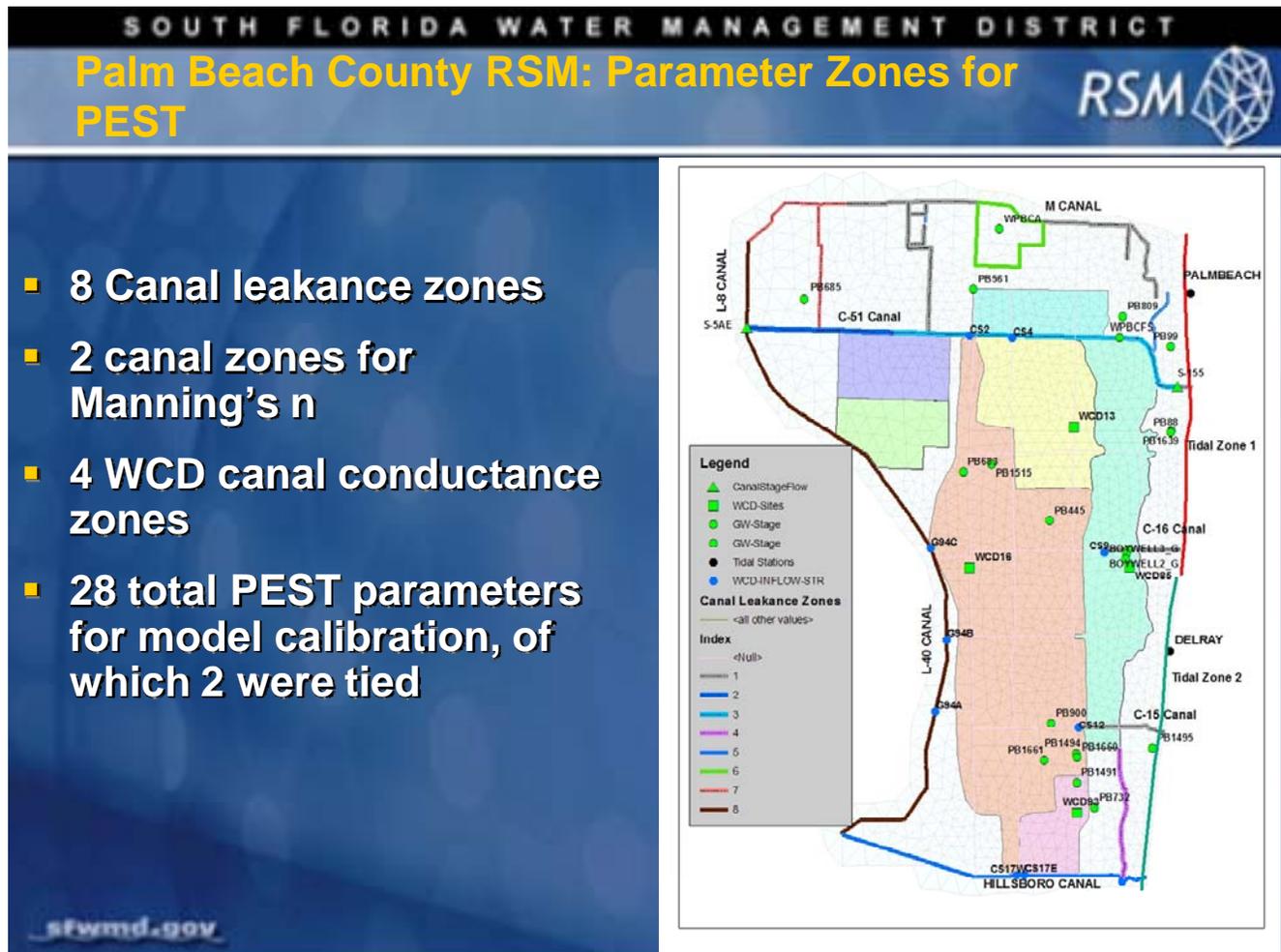
boundary, the L-40 and L-8 canals on the western boundary, the C-51, C-16 and C-15 canals. The only primary canal where flow is routed or “floated” is the C-51 canal with an upstream reach. There, historical flows were specified at the tailwater of the S5A structure (site name S5AE in DSS file), stages specified at the headwater of the G124 structure and a stage boundary condition at the headwater of the S155 structure. For all other primary canals, historical stages were fixed for all segments.

The secondary canal system in Palm Beach County is a dense network of canals maintained by local WCDs, which include Lake Worth Drainage District, the Acme Improvement District, the Loxahatchee Groves WCD, the Indian Trail Improvement District, the Northern Palm Beach Improvement District and the Seminole Water Control District.

The secondary canals and structures are modeled in RSM indirectly using WCD waterbodies and watermovers. The WCD waterbodies use a lumped equivalent storage term for all secondary canals within a WCD, which is maintained at a control elevation. The WCD watermovers interact with the groundwater system through seepage watermovers, which can be calibrated to match the observed water levels in secondary canals within the WCD waterbody. The WCD watermovers also interact with the primary canal system using water control structure watermovers which are typically genxweirs, to maintain the water level at the control elevation desired within the WCD.



The surficial aquifer in Palm Beach County is an aggregation of the unconfined sand/shell aquifer and the Biscayne aquifer. The system's most productive zone is a northern extension of the Biscayne aquifer, and is comprised primarily of highly solutioned limestone. The aquifer extends from the Palm Beach – Broward county line to north of the M canal and pinches to the west around WCA-1. For the purposes of regional simulation in RSM, the aquifer has been aggregated to a single layer and given vertically averaged aquifer properties based on a number of pump tests available in the DBHYDRO-WILMA database.



The parameters to be estimated during calibration include canal leakance to the aquifer, Manning's roughness for the canals and conductance of the WCD waterbodies that represent the secondary canals. Parameter values were estimated for all features within selected zones. The zones for canals and WCD waterbodies are shown here. In total, 29 parameters were estimated. However, two were found to be significantly correlated and thus the values were tied together by a proportionality constant.

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PEST Objective Function



$$\Phi = \sum_{i=1}^M w_i (B_i)^2 + \sum_{i=1}^M v_i (RMSE_i)^2$$

Φ = weighted sum of cumulative bias and root mean square error (RMSE) across all monitoring stations and state variables;

M = total number of monitoring sites;

w_i = weight assigned to data at site i that will be applied to bias;

v_i = weight assigned to data at site i that will be applied to RMSE;

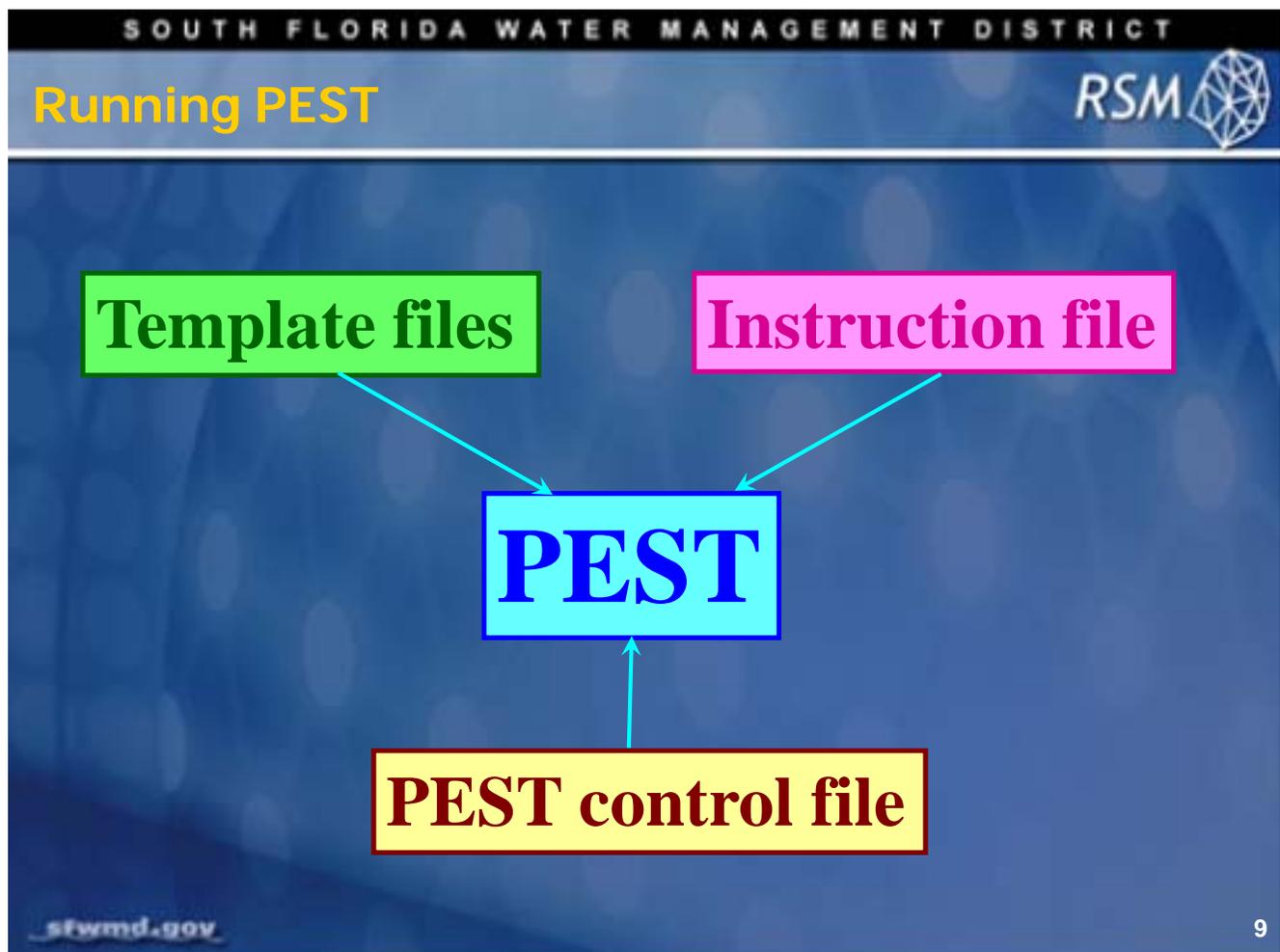
B_i = cumulative bias at site i ;

$RMSE_i$ = root mean square error at site i

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The PEST calibration is conducted by using various linear techniques to minimize the objective function. In the case of RSM, the objective function is based on the historical and simulated daily stage values for canals and groundwater wells.



Running PEST requires three sets of files;

Instruction file (*.ins):

The instruction file provides the information for the location of the output values that are compared to measured data for model optimization. For the Palm Beach County Model this is the residuals.ins file.

Template file (*.tpl):

The template files are the same as the model input files that contain the parameters that are going to be optimized, except the template files have the variable names substituted for the parameter values in the template files. There are several template files because the parameters are located in several XML files. The files are listed at the bottom of the control file **palm_24.pst**.

Control file (*.pst):

The control file (**palm_24.pst**) contains all of the parameter values used to control the operation of the PEST model run.

```

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PEST Control File: (palm_24.pst)
RSM

pcf
* control data
restart_estimation
39 176 8
6 1 single point 1 0 0
20.0 2.0 0.3 0.00003 10
3.0 3.0 0.001 2
0.1
40 0.01 4 5 0.01 3
1 1 1
* parameter groups
pb_k relative 0.01 0.0 switch 2.0 parabolic
pb_sc relative 0.01 0.0 switch 2.0 parabolic
pb_canal_n relative 0.01 0.0 switch 2.0 parabolic
pb_canal_kd relative 0.01 0.0 switch 2.0 parabolic
pb_levee_kmd relative 0.01 0.0 switch 2.0 parabolic
kturf relative 0.01 0.0 switch 2.0 parabolic
pbwcd_lc relative 0.01 0.0 switch 2.0 parabolic
pb_ghb relative 0.01 0.0 switch 2.0 parabolic
* parameter data
pb_k1 log factor 5.6818932E-06 1.7000000E-07 1.000000E-03 pb_k
pb_k2 log factor 1.7230277E-04 1.000000E-07 1.000000E-03 pb_k
pb_k3 log factor 2.4705673E-05 1.000000E-07 1.000000E-03 pb_k
pb_k4 log factor 4.5504784E-05 1.000000E-07 1.000000E-03 pb_k

```

Pest control file (.pst) used by the “pestgen” utility the very first time.

Npar- Number of parameters including adjustable, fixed and tied. $39 = 26(\text{adj}) + 2(\text{tied}) + 11(\text{fixed})$.

Npargp – Number of similar parameters grouped together.

There are 8 parameter groups including hydraulic conductivity, storage, Manning’s n, canal k/del, levee-seepage coefficient, the vegetation ET coefficients (kturf), lumped canal conductance for WCDs, and the GHB value for tidal boundary condition.

For parameter groups, ‘relative’ means the increment used for calculation of forward differences will be 0.01 times the current value.

The value for the lower increment, here set to “0.0”, is the smallest value by which the parameter can be changed for calculating derivatives.

Switch means PEST can choose between forward and central differences for derivative calculations.

2.0 is the increment for the central difference over the forward difference.

Parabolic means a parabola is fitted through the three points used to calculate the central difference and the derivative of the parabola is computed.

For each parameter, enter the current value, lower limit, upper limit and the group name.

Pest Control File

```

pb_canal_kd6 log factor 8.0072348E-06 1.000000e-08 1.000000e-03 pb_canal_kd
pb_canal_kd7 log factor 8.6172189E-04 1.000000e-08 1.000000e-03 pb_canal_kd
pb_canal_kd8 log factor 2.8442789E-04 1.000000e-08 1.000000e-03 pb_canal_kd
pb_l8_kmd log factor 5.1873338E-05 1.000000e-08 1.000000e-03 pb_lev_kmd
pb_l40n_kmd log factor 2.7655778E-05 1.000000e-08 1.000000e-03 pb_lev_kmd
pb_l40s_kmd log factor 4.8328971E-06 1.000000e-08 1.000000e-03 pb_lev_kmd
kturfq1 fixed factor 0.5400000 1.000000e-01 1.500000e+00 kturf
kturfq2 fixed factor 0.7500000 1.000000e-01 1.500000e+00 kturf
kturfq3 fixed factor 1.030000 1.000000e-01 1.500000e+00 kturf
kturfq4 fixed factor 0.8300000 1.000000e-01 1.500000e+00 kturf
pbwcd_lc1 log factor 1.3222125E-05 1.000000e-08 1.000000e-03 pbwcd_lc
pbwcd_lc2 log factor 1.0000000E-03 1.000000e-08 1.000000e-03 pbwcd_lc
pbwcd_lc3 log factor 1.2992883E-05 1.000000e-08 1.000000e-03 pbwcd_lc
pbwcd_lc4 log factor 1.0000000E-08 1.000000e-08 1.000000e-03 pbwcd_lc
pb_ghb1 tied factor 5.8329962E-04 1.000000e-07 1.000000e+05 pb_ghb
pb_ghb2 tied factor 6.4337116E-04 1.000000e-07 1.000000e+05 pb_ghb
pb_ghb1 pb_k3
pb_ghb2 pb_k1
* observation groups
ch_bias
ch_rms
sf_bias
sf_rms
sh_bias
sh_rms
wh_bias
wh_rms
* observation data

```

If there are parameters tied enter here.

The information in the “parameter data” section controls the parameter estimation process in PEST. A few of the key attributes of this file are as follows:

Enter ‘fixed’ for a parameter which does not change during PEST runs.

Enter ‘log’ for parameters which change in orders of magnitude like hydraulic conductivity.

The tied or correlated parameters should be entered after all the other parameters have been listed in this section.

Observation groups include both bias and root mean square error (RMSE) statistics for:

- groundwater stage or cell head (ch)
- canal stage or segment head (sh)
- Water Control District Stage (wh)
- canal flow or segment flow (sf)

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Pest Control File

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Initial values for the
observation data

Weights for the
observation data

wh_rms			
* observation data			
CH_BOYWELL1_G_RUN_b	0.00000	0.00000	ch_bias
CH_BOYWELL2_G_RUN_b	0.00000	0.00000	ch_bias
CH_BOYWELL3_G_RUN_b	0.00000	0.00000	ch_bias
CH_PB-1684_RUN_b	0.00000	0.00000	ch_bias
CH_PB1491_RUN_b	0.00000	0.00000	ch_bias
CH_PB1494_RUN_b	0.00000	1.00000	ch_bias
CH_PB1495_RUN_b	0.00000	1.00000	ch_bias
CH_PB1515_RUN_b	0.00000	1.00000	ch_bias
CH_PB1639_RUN_b	0.00000	1.00000	ch_bias
CH_PB1660_RUN_b	0.00000	1.00000	ch_bias
CH_PB1661_RUN_b	0.00000	1.00000	ch_bias
CH_PB445_RUN_b	0.00000	1.00000	ch_bias
CH_PB561_RUN_b	0.00000	1.00000	ch_bias

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For calibration, 176 “observations” are used which include cell heads (CH), segment heads (SH), segment flows (SF) and WCD heads (WH) including both bias and RMSE. Both bias and RMSE have the same weight for stage data. Zero values for weights tell PEST not to use this observation in the objective function. This is useful when configuring different PEST calibration runs.

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Observations and Weights

- The PEST documentation suggests that weights for each observation should be inversely proportional to the standard deviations of the observations - weights should be an indicator of the accuracy or reliability of the data
- If observations are of different types like stage and flow, the weights assigned should reflect the magnitudes of the two quantities
- Weights should be chosen such that the contribution to the objective function for each measurement is equitable

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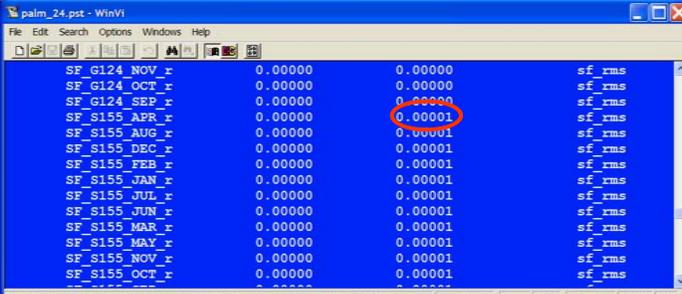
The flow monitoring sites were weighted with lower values to account for the magnitude of flow values. Again, due to the uncertainty of the flow data reported as pump logs for secondary WCDs, the weights were much less in magnitude as compared to the weights for primary canals where flow is computed based on the breakpoint data. The choice of weights for PEST calibration took into consideration the quality of the data. It was a trial and error procedure involving many initial PEST runs.

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Pest Control File

Weights for flows should reflect the magnitudes



SF_G124_NOV	r	0.00000	0.00000	sf_rms
SF_G124_OCT	r	0.00000	0.00000	sf_rms
SF_G124_SEP	r	0.00000	0.00000	sf_rms
SF_S155_APR	r	0.00000	0.00001	sf_rms
SF_S155_AUG	r	0.00000	0.00001	sf_rms
SF_S155_DEC	r	0.00000	0.00001	sf_rms
SF_S155_FEB	r	0.00000	0.00001	sf_rms
SF_S155_JAN	r	0.00000	0.00001	sf_rms
SF_S155_JUL	r	0.00000	0.00001	sf_rms
SF_S155_JUN	r	0.00000	0.00001	sf_rms
SF_S155_MAR	r	0.00000	0.00001	sf_rms
SF_S155_MAY	r	0.00000	0.00001	sf_rms
SF_S155_NOV	r	0.00000	0.00001	sf_rms
SF_S155_OCT	r	0.00000	0.00001	sf_rms

+V:\sfrsm\workdir\submodels\palmbeach\pcluster\pest\palm_24.pst [LF] 258 lines, i Num |--72%-- 00186 064

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The flow values are much higher than stage values and thus the weights for the flow observations are high in order that the flows and stages are similarly valued in the objective function.

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Pest Control File

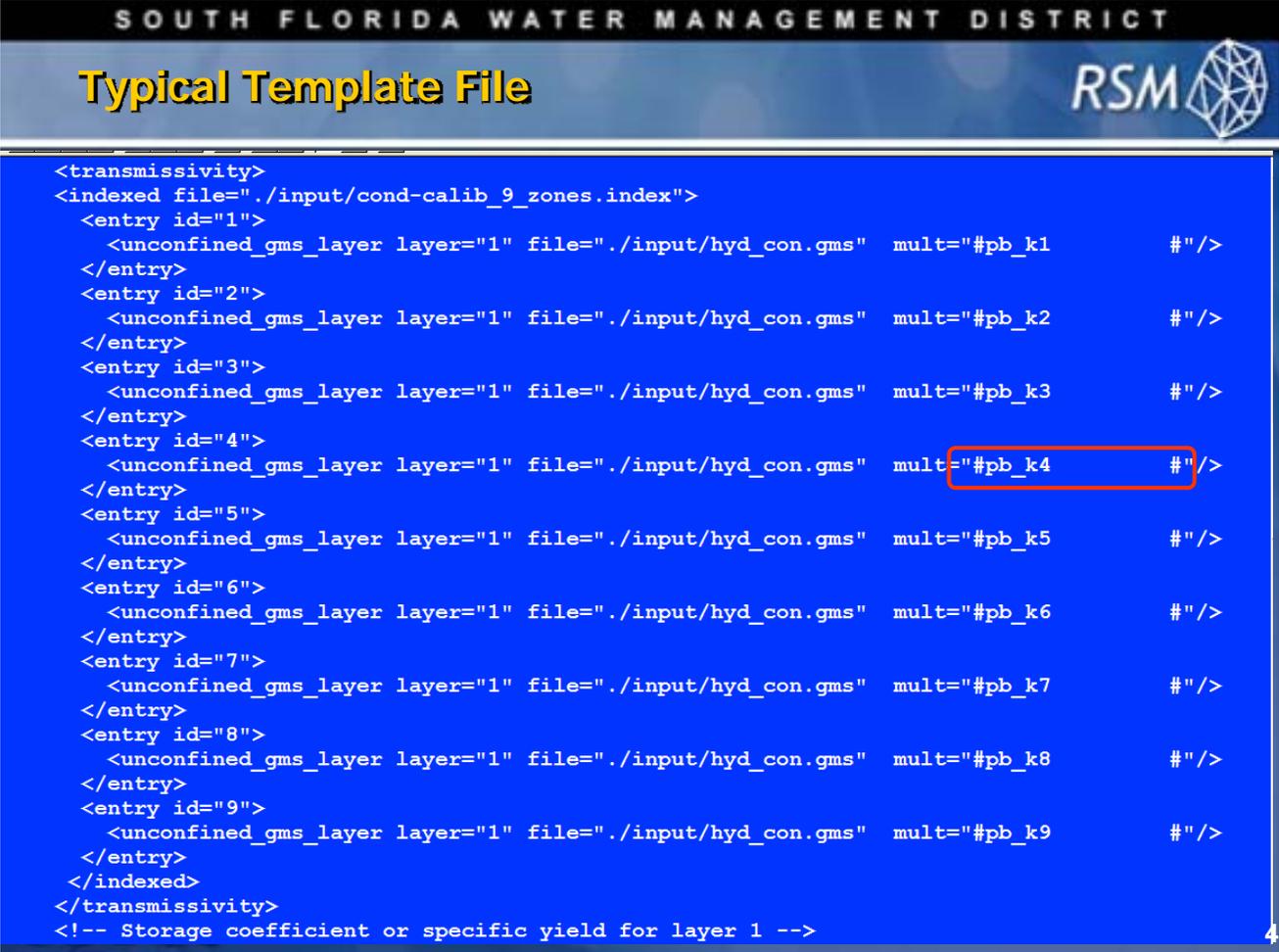
```

SF_DEMAND_SEP_r      0.00000      0.0000010      sf_rms
SF_DEMAND_OCT_r     0.00000      0.0000010      sf_rms
SF_DEMAND_NOV_r     0.00000      0.0000010      sf_rms
SF_DEMAND_DEC_r     0.00000      0.0000010      sf_rms
* model command line
./run_it.sh
* model input/output
run_calib_pb_9kzones_9canalindex.xml.tpl run_calib_pb_wcd_wm_weirs.xml
pb_levee-seepage.xml.tpl pb_levee-seepage.xml
wcd_waterbodies.xml.tpl wcd_waterbodies.xml
et_kc_quarterly.dat.tpl et_kc_quarterly.dat
tide_wallghb_011506.xml.tpl tide_wallghb_011506.xml
evap_prop_10_04_05.xml.tpl.tpl evap_prop_10_04_05.xml.tpl
residuals.ins residuals.out
* prior information

```

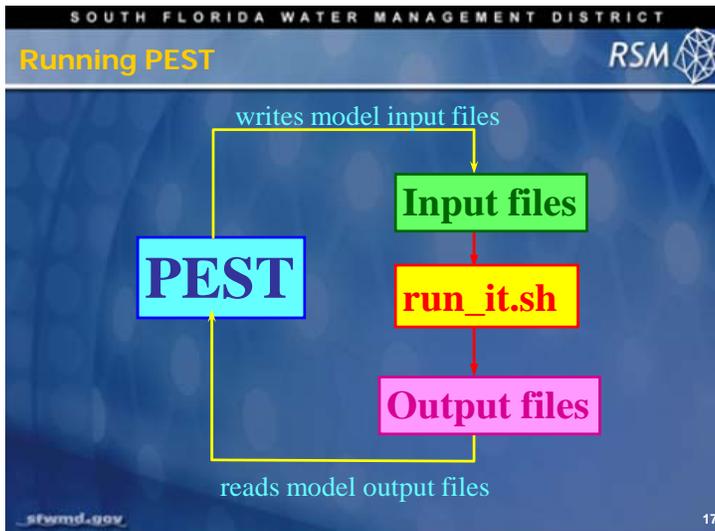
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Template files are used to define the input files whose parameters get updated by PEST. The run_it.sh shell script runs the HSE along with Python scripts used in calculation of residuals. The last part of the control file lists the command lines to run the RSM. A template file is used for each of the parameter input files along with data files when the XML file has parameters which change with every PEST run. In this run there are six template files.



```
<transmissivity>
<indexed file="./input/cond-calib_9_zones.index">
  <entry id="1">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k1      #"/>
  </entry>
  <entry id="2">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k2      #"/>
  </entry>
  <entry id="3">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k3      #"/>
  </entry>
  <entry id="4">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k4      #"/>
  </entry>
  <entry id="5">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k5      #"/>
  </entry>
  <entry id="6">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k6      #"/>
  </entry>
  <entry id="7">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k7      #"/>
  </entry>
  <entry id="8">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k8      #"/>
  </entry>
  <entry id="9">
    <unconfined_gms_layer layer="1" file="./input/hyd_con.gms" mult="#pb_k9      #"/>
  </entry>
</indexed>
</transmissivity>
<!-- Storage coefficient or specific yield for layer 1 -->
```

The template file is used to define place holders for the conductivity values for the 9 hydraulic conductivity zones where the values are enclosed in double quotes. In this case before PEST runs, the PEST program will replace the strings “#pb_k1#”, “#pb_k2#” “#pb_k9#” with the current values of the parameters.



PEST creates the input files for the RSM model. The script `run_it.sh` runs the RSM and post-processes the results to create the file containing the bias and RMSE values. PEST uses those values to estimate the parameter values for the next iteration.

```

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Running PEST
RSM

writes model input files
Input files
PEST
run_it.sh
Output files
reads model output files
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```

```

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Script Runs HSE: run_it.sh
RSM

#!/bin/sh
# -S /bin/bash

# Clean up my mess...
rm job_id.txt et_monthly_kc.par evap_prop_10_04_05.xml input output/*
# In case I die...
echo $JOB_ID > ./job_id.txt

# Intermediate processing
ln -s ../../input ./input
/opt/local/share2/bin/python ../bin/make-monthly-crop-coeff.py et_kc_quarterly.dat et_kc_monthly.par
/opt/local/share2/bin/tempchek evap_prop_10_04_05.xml.tpl evap_prop_10_04_05.xml et_kc_monthly.par
# Run the Big Kabona
./bin/hse_run_calib_pb_wod_wm_weirs.xml >& /dev/null
# Retrieve residuals
export DISPLAY=:1.1
/opt/local/share2/bin/dssvue ../bin/post_process.py
/opt/local/share2/bin/dssvue ../bin/calcStats.py ../bin/fetch-calib.cti >& /dev/null
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```

Obtaining the optimal set of parameter values from PEST will require many iterations using the parameter upgrade vector. Each iteration will require “n” runs. To complete a calibration exercise, PEST is run in parallel on a Linux processor cluster with multiple CPUs and common RAM and storage. A temporary directory is setup for each processor. The directory includes the input and template files and `run_it.sh` script. This script runs the RSM implementation and creates the necessary statistics (bias and RMSE) for the objective function.

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Input File used by Script to Calculate Residuals RSM 

Residuals calculated from the `fetch_calib.ctl` file used to specify the dss paths of the historical observed data

```

File  ./output/gbstageov.dss  ../final_run_palm_7/output/gbstageov.dss  ../final_run_palm_7/output/gbstageov.dss
run   CH_G124TW  /SFWMD/G124TW/STAGE//1DAY/SIM/  /SFWMD/G124TW/STAGE//1DAY/HISTORICAL/  /SFWMD/G
run   CH_WFBCA  /SFWMD/WFBCA/STAGE//1DAY/SIM/  /SFWMD/WFBCA/STAGE//1DAY/OBS/  /SFWMD/W
run   CH_PB561  /SFWMD/PB561/STAGE//1DAY/SIM/  /SFWMD/PB561/STAGE//1DAY/HIST_MODEL/  /SFWMD/P
run   CH_PB1461 /SFWMD/PB1461/STAGE//1DAY/SIM/  /SFWMD/PB1461/STAGE//1DAY/HIST_MODEL/  /SFWMD/P
run   CH_PB809  /SFWMD/PB809/STAGE//1DAY/SIM/  /SFWMD/PB809/STAGE//1DAY/HIST_MODEL/  /SFWMD/P
run   CH_WFBCFS  /SFWMD/WFBCFS/STAGE//1DAY/SIM/  /SFWMD/WFBCFS/STAGE//1DAY/HIST_MODEL/  /SFWMD/W
run   CH_PB1515 /SFWMD/PB1515/STAGE//1DAY/SIM/  /SFWMD/PB1515/STAGE//1DAY/HIST_MODEL/  /SFWMD/P
run   CH_PB883  /SFWMD/PB883/STAGE//1DAY/SIM/  /SFWMD/PB883/STAGE//1DAY/HIST_MODEL/  /SFWMD/P
run   CH_PB685  /SFWMD/PB685/STAGE//1DAY/SIM/  /SFWMD/PB685/STAGE//1DAY/HIST_MODEL/  /SFWMD/P
run   CH_PB99  /SFWMD/PB99/STAGE//1DAY/SIM/  /SFWMD/PB99/STAGE//1DAY/HIST_MODEL/  /SFWMD/P

```

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The residuals or the difference between observed and model computed is calculated using a script which reads the DSS file of the observed data and the path of the DSS file is specified in the `fetch_calib.ctl` file.

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Monitoring the Progress of PEST RSM 

- Objective Function
- Jacobian Matrix
- Covariance/Correlation Matrix
- Eigenvalues/eigenvectors
- Matrix Condition Number
- Parameter Sensitivities
- Parameter values and confidence intervals

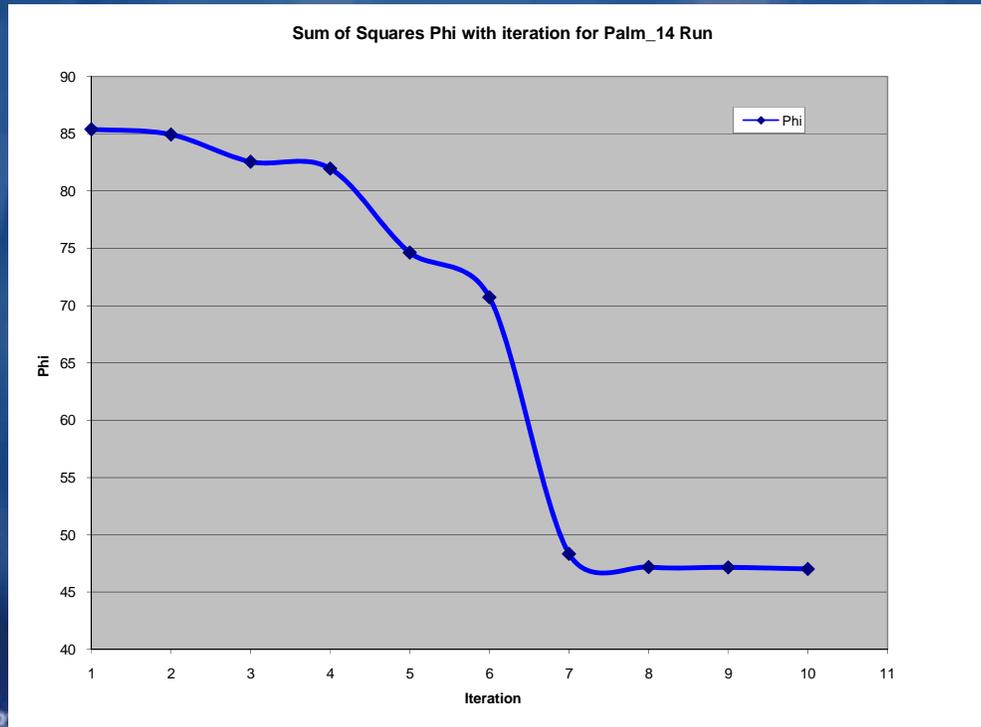
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While PEST is running, the objective function, matrix condition number, parameter sensitivities and Jacobian matrix can be viewed. The covariance/correlation matrix and eigenvalues/vectors can be viewed only after the PEST run is complete.

Objective Function



- Objective function Phi should reduce with each PEST run



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Check the Phi values in the PEST run record file by using the “grep” command.

For Palm Beach County Run 14, the biggest reduction in Phi was from iteration 6 to 7.

PEST Optimization is terminated when the objective function values are within 0.01 for the last 3 iterations.

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Jacobian Matrix: RSM 

$$J_{i,j} = \partial o_i / \partial b_j$$

$\partial o_1 / \partial b_1$	$\partial o_1 / \partial b_2$	$\partial o_1 / \partial b_3$	$\partial o_1 / \partial b_4$
$\partial o_2 / \partial b_1$	$\partial o_2 / \partial b_2$	$\partial o_2 / \partial b_3$	$\partial o_2 / \partial b_4$
$\partial o_3 / \partial b_1$	$\partial o_3 / \partial b_2$	$\partial o_3 / \partial b_3$	$\partial o_3 / \partial b_4$
$\partial o_4 / \partial b_1$	$\partial o_4 / \partial b_2$	$\partial o_4 / \partial b_3$	$\partial o_4 / \partial b_4$
$\partial o_5 / \partial b_1$	$\partial o_5 / \partial b_2$	$\partial o_5 / \partial b_3$	$\partial o_5 / \partial b_4$
$\partial o_6 / \partial b_1$	$\partial o_6 / \partial b_2$	$\partial o_6 / \partial b_3$	$\partial o_6 / \partial b_4$
$\partial o_7 / \partial b_1$	$\partial o_7 / \partial b_2$	$\partial o_7 / \partial b_3$	$\partial o_7 / \partial b_4$
$\partial o_8 / \partial b_1$	$\partial o_8 / \partial b_2$	$\partial o_8 / \partial b_3$	$\partial o_8 / \partial b_4$
etc.			

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Jacobian matrix is the derivative matrix and is the rate of change of the computed value at the observation point with respect to the parameter. Derivatives are calculated only for adjustable parameters and not for fixed or tied parameters. The simplest way to calculate a derivative is to use the forward difference method. This is done by adding an increment to the current value, unless the current value is at its upper bound, in which case the value is subtracted. Central difference gives more accurate derivative values than forward difference, but requires two model runs, and is required when the

objective function minimum is approached. The most time-consuming part of PEST is by far the calculation of the derivatives.

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Jacobian Matrix: Usage RSM 

Predicted model response to changes in parameters

$$\mathbf{c} = \mathbf{c}_o + \mathbf{J}(\mathbf{b} - \mathbf{b}_o)$$

$$\mathbf{u} = (\mathbf{J}^T \mathbf{Q} \mathbf{J})^{-1} \mathbf{J}^T \mathbf{Q} (\mathbf{c} - \mathbf{c}_o)$$

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The Jacobian matrix is used to calculate the model response to changes in the parameters and the parameter upgrade vectors.

\mathbf{J} is an $m \times n$ matrix, $\mathbf{J} \mathbf{J}$ is an $n \times n$ matrix which can be inverted. $\text{Inv}(\mathbf{J} \mathbf{J}) \mathbf{J}'$ is an $n \times m$ matrix. \mathbf{b} is the parameter vector of n values and \mathbf{c} is the vector of m model calculated observations. \mathbf{Q} is the diagonal matrix of weights.

Jacobian Matrix



- PEST writes the jacobian values in binary form into a file palm_24.jco
- Use jacwrit utility to convert the binary file to ASCII text.
 - `jacwrit palm_24.jco palm_24.jac.txt`

	pb_k1	pb_k2	pb_k3	pb_k4	pb_k5
	pb_k9	pb_canal_n2	pb_canal_n3	pb_canal_kd1	pb_canal_kd2
	pb_canal_kd6	pb_canal_kd7	pb_canal_kd8	pb_18_kmd	pb_140n_kmd
	pbwcd_lc3	pbwcd_lc4			
ch_boywell11_g_run_b	-5.036907E-02	-3.517201E-02	3.977712E-02	1.675131E-02	0.154964
	8.404440E-03	0.352000	-0.430000	-0.240850	5.238379E-03
	7.425836E-03	-1.496681E-02	-1.191587E-02	1.162805E-02	2.101108E-02
	0.102177	9.210340E-02			
ch_boywell12_g_run_b	-5.059933E-02	-3.517201E-02	3.994981E-02	1.703913E-02	0.155252
	8.462005E-03	0.356000	-0.427500	-0.239699	5.295944E-03
	7.540965E-03	-1.502437E-02	-1.203100E-02	1.168561E-02	2.112621E-02
	0.102062	9.279418E-02			
ch_boywell13_g_run_b	-0.142588	-9.952930E-02	0.104710	4.881480E-02	0.441463
	2.365908E-02	1.01900	-1.30000	-0.270093	1.427602E-02
	2.083839E-02	-4.426721E-02	-3.344504E-02	3.292695E-02	6.055796E-02
	0.291623	0.265718			

After converting the binary palm_24.jco file to text, use the text editor to view it.

The screenshot displays the RSM GUI interface. At the top, the text reads "SOUTH FLORIDA WATER MANAGEMENT DISTRICT" and "RSM". The main title is "Jacobian/Correlation Matrix: Graphic Output". The interface shows several windows:

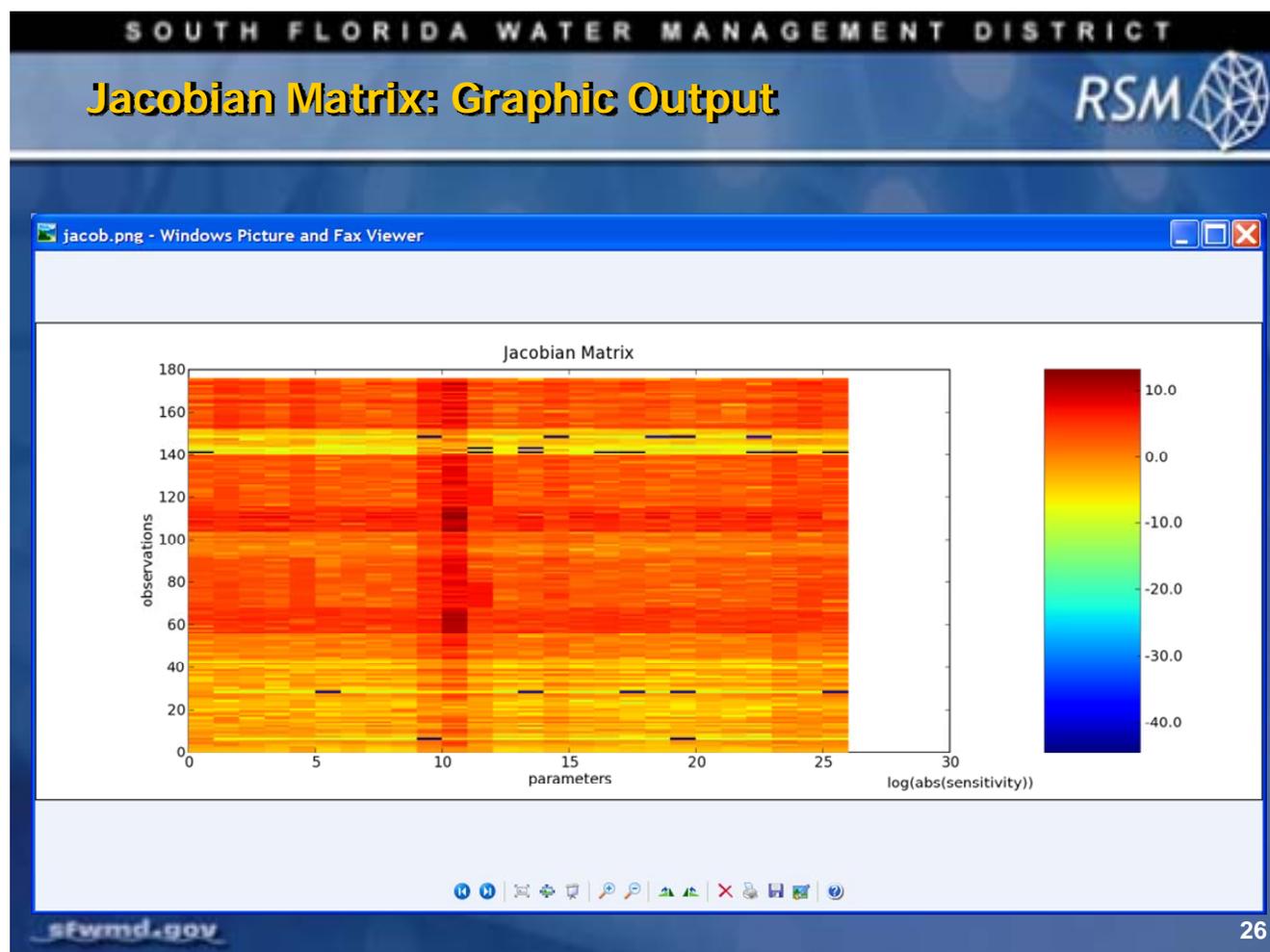
- The RSM GUIver 4.0.3 running on server: whqoom01d**: This window contains a toolbar with options like "File", "PreProcessing", "Run Model", "View Model Results", "Process Model Output", "Output Graphics", "Cluster Tools", and "Help". A "Results Viewer" panel is visible, listing various model components such as "HecDssVue", "DssMapVue", "Open IXX", "Cell Comparison Hydrographs", "Waterbody_CAT", "Waterbody_PLOT", "Watermover_CAT", "Watermover_PLOT", "Google KMZ Animation", and "Transect Tool".
- Results Viewer**: This window shows a map of a watershed with a grid overlay. A "Tools" menu is open, listing options like "Digitize ROI", "Cell Colorflood Tools", "Time Tools", "Misc Tools", "Segment Colorflood Tools", and "Change Flow Vector Grid Size". The "Misc Tools" menu is further expanded, showing options like "Movie", "Calibration", "Hydrograph", "Segment viewer", "Summary Statistics", and "Pest Visualization".
- Pest Visualization**: This window is open, showing a table for "PEST Calibration Results". The table has three rows, each with a "Parameter:" label and a "number" value. Below the table are three buttons: "Import Jacobian File", "Import Correlation File", and "Exit".

A large blue arrow points from the "Pest Visualization" window towards the bottom right of the screen.

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The Jacobian/correlation matrix can be saved as a graphic output using the RSM GUI toolbar. Start the RSM GUI and from Tools->Misc Tools->Pest Visualization->import Pest Jacobian/Correlation->File-Save as PNG



The Jacobian values can be viewed graphically using the RSM GUI utility. This is used to identify parameters and observations that are highly correlated and thus do not help obtain an optimal solution.

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Covariance Matrix: Hydraulic Conductivity RSM 

	pb_k3	pb_k4	pb_k5	pb_k6	pb_k7
pb_k1	0.0071936	-0.0430110	-0.0137700	-0.0274780	-0.0425900
pb_k2	0.0117970	0.0130140	-0.1550000	0.2484000	0.2942000
pb_k3	0.0467880	0.0032930	-0.0766910	0.0155540	0.0426090
pb_k4	0.0032930	2.3330000	-0.6096000	0.9954000	-1.1760000
pb_k5	-0.0766910	-0.6096000	0.6329000	-0.6192000	0.1448000
pb_k6	0.0155540	0.9954000	-0.6192000	3.1630000	-0.6184000
pb_k7	0.0426090	-1.1760000	0.1448000	-0.6184000	6.1580000
pb_k8	0.0412130	-0.5532000	-0.1785000	0.0794870	1.6980000
pb_k9	-0.0162360	-0.3164000	0.1059000	-0.0156360	0.2615000

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Diagonal elements of the matrix are the variances of the calculated results at the observation points. Diagonal elements with the largest variances are the ones with the highest uncertainty. The parameters pb_k7 and pb_k6 have the highest variances.

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Covariance: Manning's n RSM 

	pb_canal_n2	pb_canal_n3
pb_canal_n2	0.0138840	-0.0000756
pb_canal_n3	-0.0000756	0.0001539

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The Manning's n roughness values for the two canal groups are not correlated.

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Covariance for Canal k/del RSM 

	pb_canal_kd1	pb_canal_kd2	pb_canal_kd3	pb_canal_kd4
pb_canal_kd1	0.7753000	0.6988000	0.9716000	0.0223180
pb_canal_kd2	0.6988000	9.0580000	2.3910000	-0.8400000
pb_canal_kd3	0.9716000	2.3910000	3.2010000	0.4088000
pb_canal_kd4	0.0223180	-0.8400000	0.4088000	0.4453000
pb_canal_kd5	1.3690000	1.1350000	2.7870000	0.9968000
pb_canal_kd6	-0.0064404	0.3041000	-0.6325000	-0.3201000
pb_canal_kd7	-0.9746000	-5.7090000	-5.5100000	-1.4090000
pb_canal_kd8	1.6850000	4.0560000	2.7540000	-0.2500000

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There is a high covariance between some of the canal-aquifer interaction terms (k/del).

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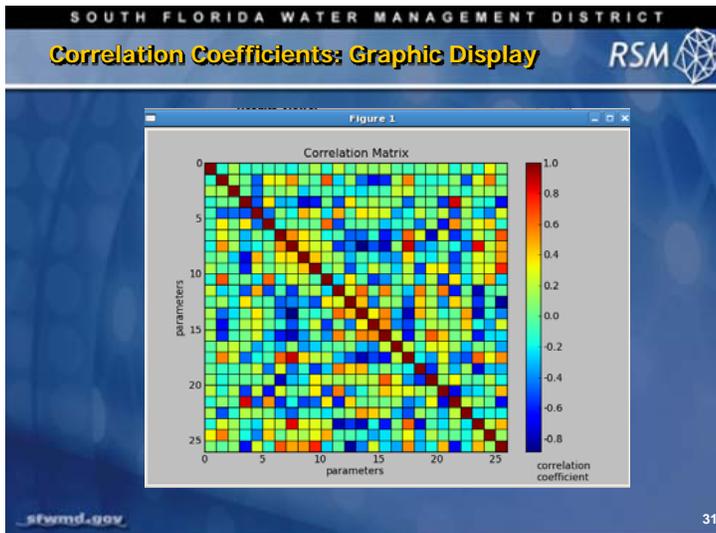
Correlation Coefficient RSM 

- Parameter correlation is at least as important as examining individual parameter sensitivities.
- Off-diagonal terms will range from -1 to 1, depending on the degree of correlation.
- Values near zero, are desirable because they indicate absence of correlation.
- Values close to 1 or -1 are less desirable because they indicate the parameters are strongly correlated.

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Correlated parameters are parameters that can be varied in groups with little effect on model output and therefore little effect on the objective function. If PEST is having difficulty in reducing the objective function in one of your models, check the degree of parameter correlation. If you find that parameters are strongly correlated, PEST is providing valuable feedback on your observation data that might not have been noticed otherwise. Specifically, you've learned that additional observations are required to resolve the parameters. In many circumstances, heads by themselves

are inadequate for resolving model non-uniqueness. You will have better luck in calibrating transport models if you also have observations of flow and/or concentration.



The graphic display of the correlation coefficients created by the Rsmtoolbar (corrln.png) shows the parameters that are highly correlated, both positively and negatively. The dark colored off diagonal elements show very high correlations.

	pb_k1	pb_k2	pb_k3	pb_k4
pb_k1	1.000	-0.4960	-2.2512E-02	0.2581
pb_k2	-0.4960	1.000	0.1412	-0.2952
pb_k3	-2.2512E-02	0.1412	1.000	0.1648
pb_k4	0.2581	-0.2952	0.1648	1.000

Open the PEST record file (palm_24.rec) to look at the correlation coefficients for parameters. The parameters pb_k1 and pb_ghb2 are highly correlated as well as pb_k3 and pb_ghb1. This is likely because pb_k1 is the groundwater conductivity associated with the general head boundary condition used in pb_ghb2, and similarly for pb_k3 and pb_ghb2.

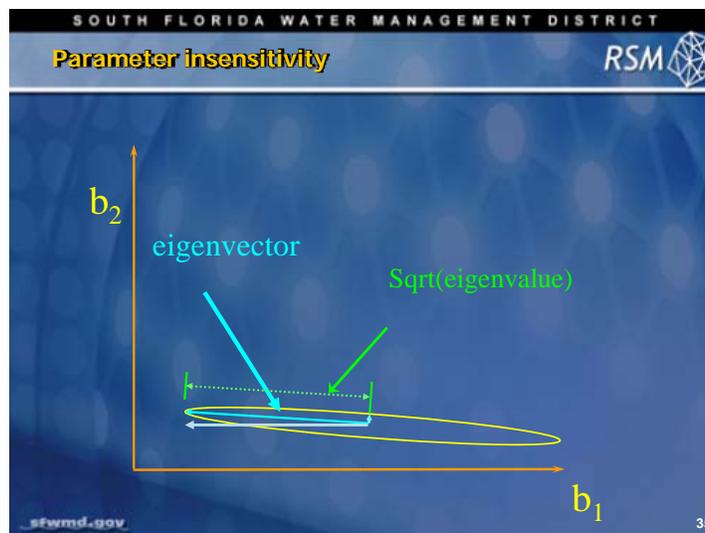
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Eigenvector and Eigenvalues RSM 

- Eigenvectors are actually a way to learn about parameter correlation between more than two parameters.
- If the model is insensitive to a single parameter, the eigenvector corresponding to the largest eigenvalue will be dominated by a single component, this pertaining to the insensitive parameter.
- However, if the eigenvector has a number of significant components rather than one, it is an indication of insensitivity associated with a group of parameters (ie. parameter correlation).
- Correlated parameters are those whose eigenvector components are significantly non-zero.

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The eigenvectors and eigenvalues provide useful information about which parameters are important and which parameters are causing problems in the calibrations.



The highest eigenvalue is the direction in the parameter space where the estimation is the weakest. The eigenvector components of largest eigenvalue are dominated by a single component. Normally the highest eigenvalue is the most important because this is the direction in parameter space in which parameters are most poorly estimated, i.e. the probability ellipsoid is longest in this direction. Looking to the eigenvector corresponding to the highest eigenvalue, we can often see at a glance what may be causing problems in parameter estimation. If the model is insensitive to a

single parameter, the eigenvector corresponding to the largest eigenvalue will be dominated by a single component, this pertaining to the insensitive parameter.

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Eigenvalues																											
RSM																											
	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	AA
1		Vector_1	Vector_2	Vector_3	Vector_4	Vector_5	Vector_6	Vector_7	Vec	Vi	Ve	Ve	VV	Vector_25	Vector_26												
2	pb_k1	0.00106	-0.01502	0.02812	0.01283	-0.10890	0.07930	-0.40900	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.00794	0.00003
3	pb_k2	-0.01055	0.04339	-0.03352	-0.19410	-0.09856	0.32270	-0.41520	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.03890	0.01590
4	pb_k3	0.00106	-0.02500	-0.02551	-0.08809	0.01247	-0.16050	0.10950	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.00526	0.00511
5	pb_k4	-0.00038	0.05027	0.01732	-0.19200	-0.19830	-0.04615	0.05414	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.09435	-0.14670
6	pb_k5	-0.00248	0.00426	-0.03926	-0.02244	0.05714	-0.09796	-0.01949	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.08122	0.01743
7	pb_k6	-0.00356	-0.01182	-0.00526	0.07738	-0.09464	0.08659	-0.02917	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.22460	-0.08676
8	pb_k7	0.00178	0.00927	-0.04842	-0.10090	0.13300	-0.10360	-0.02257	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.02897	0.33780
9	pb_k8	-0.00710	-0.01026	-0.08904	0.16520	-0.79220	0.22920	0.06201	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.17190	0.12640
10	pb_k9	0.00184	0.02670	-0.00580	-0.16490	-0.05965	-0.21940	0.11620	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.00252	0.02264
11	pb_canal_n2	0.06480	-0.93510	-0.26110	-0.18960	-0.02951	0.00603	0.02296	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.00075	0.00525
12	pb_canal_n3	0.99740	0.07038	-0.00365	-0.00255	-0.00701	0.00396	-0.00460	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.00125	-0.00040
13	pb_canal_kd1	0.00495	-0.08564	0.60550	-0.13270	-0.35550	-0.42760	0.00705	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.16420	0.00800
14	pb_canal_kd2	-0.00107	0.00714	0.05703	-0.08588	0.07159	0.22060	0.09591	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.13660	-0.27600
15	pb_canal_kd3	-0.00637	0.04193	0.02456	-0.30930	-0.00429	0.13830	0.11330	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.23780	-0.14350
16	pb_canal_kd4	0.02236	-0.24990	0.54900	0.48480	0.12020	0.44400	0.11450	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.03404	-0.02603
17	pb_canal_kd5	-0.00332	0.03767	-0.07514	-0.17560	-0.20250	0.13030	0.03742	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.36390	-0.22300
18	pb_canal_kd6	0.00367	0.00702	0.05014	-0.05874	0.10850	0.13920	0.08769	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.01028	-0.01340
19	pb_canal_kd7	0.00063	-0.02312	0.06669	-0.02400	0.05672	-0.00260	0.03769	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.33480	0.49690
20	pb_canal_kd8	0.00208	-0.04676	-0.01149	0.13470	-0.07007	0.04089	-0.04539	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.46920	0.07655
21	pb_l8_kmd	0.00119	-0.01618	0.00913	0.13650	0.04766	-0.09023	-0.07808	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.00718	-0.35410
22	pb_l40n_kmd	-0.00131	0.00343	-0.00564	-0.04225	0.05195	0.02466	0.00634	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.34950	0.23070
23	pb_l40s_kmd	-0.00137	-0.01513	0.04159	-0.05834	0.04140	-0.05858	0.03707	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.43240	-0.49110
24	pbwcd_lc1	0.00082	0.04028	-0.03619	0.05146	-0.21750	-0.11090	-0.20490	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.01261	-0.02244
25	pbwcd_lc2	0.00474	-0.05871	0.45900	-0.54290	0.05026	0.18390	-0.03850	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.15470	0.04708
26	pbwcd_lc3	0.00189	0.01718	-0.03804	0.05485	-0.11420	-0.04810	0.68140	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.01474	0.00343
27	pbwcd_lc4	-0.01405	0.18060	-0.13110	-0.27830	-0.02357	0.43220	0.25040	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.01886	0.13060
28																											
29	Max	0.99740	0.18060	0.60550	0.48480	0.13300	0.44400	0.68140	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	0.43240	0.49690
30	Min	-0.01405	-0.93510	-0.26110	-0.54290	-0.79220	-0.42760	-0.41520	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	-0.46920	-0.49110
31																											
32	Eigenvalues	0.00001	0.00015	0.00040	0.00229	0.00479	0.00886	0.01218	###	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	##	24.62000	41.64000
33	Ratio	8.06E+06																									

Shown are the eigenvectors and eigenvalues for the Palm Beach County Model. The columns are the eigenvectors. Vectors1, Vector2 ... Vector26. The largest eigenvalue is 41.64 and the eigenvector corresponding to this has 4 components shown in color. These groups of parameters are somewhat insensitive. A similar pattern is seen for the next highest eigenvalue corresponding to 24.62

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Eigenvalues RSM 

- If the ratio of the highest to the lowest eigen value is $> 10^8$ then there is a strong possibility that PEST is having difficulty calculating the parameter upgrade vector due to parameter insensitivity or correlation.
- The square root of the ratio is related to the “condition number” of the matrix that PEST must invert when solving for the parameter upgrade.
- Palm Beach Case – Eigen Values:

9.1695E-06	1.5424E-04	4.0495E-04	2.2877E-03	4.7866E-03	8.8631E-03
1.2184E-02	1.6076E-02	1.6498E-02	2.8623E-02	3.7183E-02	4.4083E-02
5.0725E-02	6.4151E-02	9.1504E-02	0.1217	0.2625	0.3577
0.7163	1.483	1.970	4.939	7.307	21.40
41.64]					24.62
- Ratio was 8.06e+06 (10^7) – somewhat borderline.

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Condition numbers indicate how well-posed the calibration problem is.

Large condition numbers indicate the matrix is ill-conditioned.

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Condition numbers RSM 

Matrix Condition Numbers during PEST run

Use the grep command to search for 'CONDITION' in the palm_24.cnd file

The Condition numbers should preferably be less than 104.

```

RECORD OF "NORMAL MATRIX" CONDITION NUMBERS: CASE palm_24
MATRIX CONDITION NUMBERS = 120.15
MATRIX CONDITION NUMBERS = 120.15
MATRIX CONDITION NUMBERS = 104.21
MATRIX CONDITION NUMBERS = 121.10
MATRIX CONDITION NUMBERS = 138.10
MATRIX CONDITION NUMBERS = 13.125
MATRIX CONDITION NUMBERS = 11.188
MATRIX CONDITION NUMBERS = 20.257
MATRIX CONDITION NUMBERS = 39.106
MATRIX CONDITION NUMBERS = 36.789
MATRIX CONDITION NUMBERS = 54.533
MATRIX CONDITION NUMBERS = 11.687
MATRIX CONDITION NUMBERS = 11.423
MATRIX CONDITION NUMBERS = 12.053
MATRIX CONDITION NUMBERS = 12.243
MATRIX CONDITION NUMBERS = 11.412
MATRIX CONDITION NUMBERS = 10.961
MATRIX CONDITION NUMBERS = 10.511
MATRIX CONDITION NUMBERS = 23.425
MATRIX CONDITION NUMBERS = 22.657
MATRIX CONDITION NUMBERS = 24.799
MATRIX CONDITION NUMBERS = 24.989
MATRIX CONDITION NUMBERS = 26.934
MATRIX CONDITION NUMBERS = 27.458
MATRIX CONDITION NUMBERS = 27.931
MATRIX CONDITION NUMBERS = 28.030
MATRIX CONDITION NUMBERS = 28.130
MATRIX CONDITION NUMBERS = 28.180
MATRIX CONDITION NUMBERS = 16.659
MATRIX CONDITION NUMBERS = 16.598
MATRIX CONDITION NUMBERS = 16.484
MATRIX CONDITION NUMBERS = 16.281
MATRIX CONDITION NUMBERS = 12.044
MATRIX CONDITION NUMBERS = 12.042
MATRIX CONDITION NUMBERS = 12.009
MATRIX CONDITION NUMBERS = 11.968
MATRIX CONDITION NUMBERS = 6.6503
MATRIX CONDITION NUMBERS = 6.6536
MATRIX CONDITION NUMBERS = 6.7724
  
```

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If the condition number of a matrix is around 1, it is well-conditioned.

If the condition number of a matrix is 10^5 , it is ill-conditioned.

PEST has to work hard when a condition number is large to find a solution.

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Parameter Sensitivity RSM 

- Parameter sensitivity derived from the Jacobian matrix.
- Composite parameter sensitivities written to the palm_24.sen file.
- Relative composite sensitivity of a parameter obtained by multiplying its composite value by the magnitude of the value of the parameter.

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It is important to review the parameter sensitivities to identify those parameters that are insensitive and thus inhibit the effectiveness of PEST to obtain a good solution.

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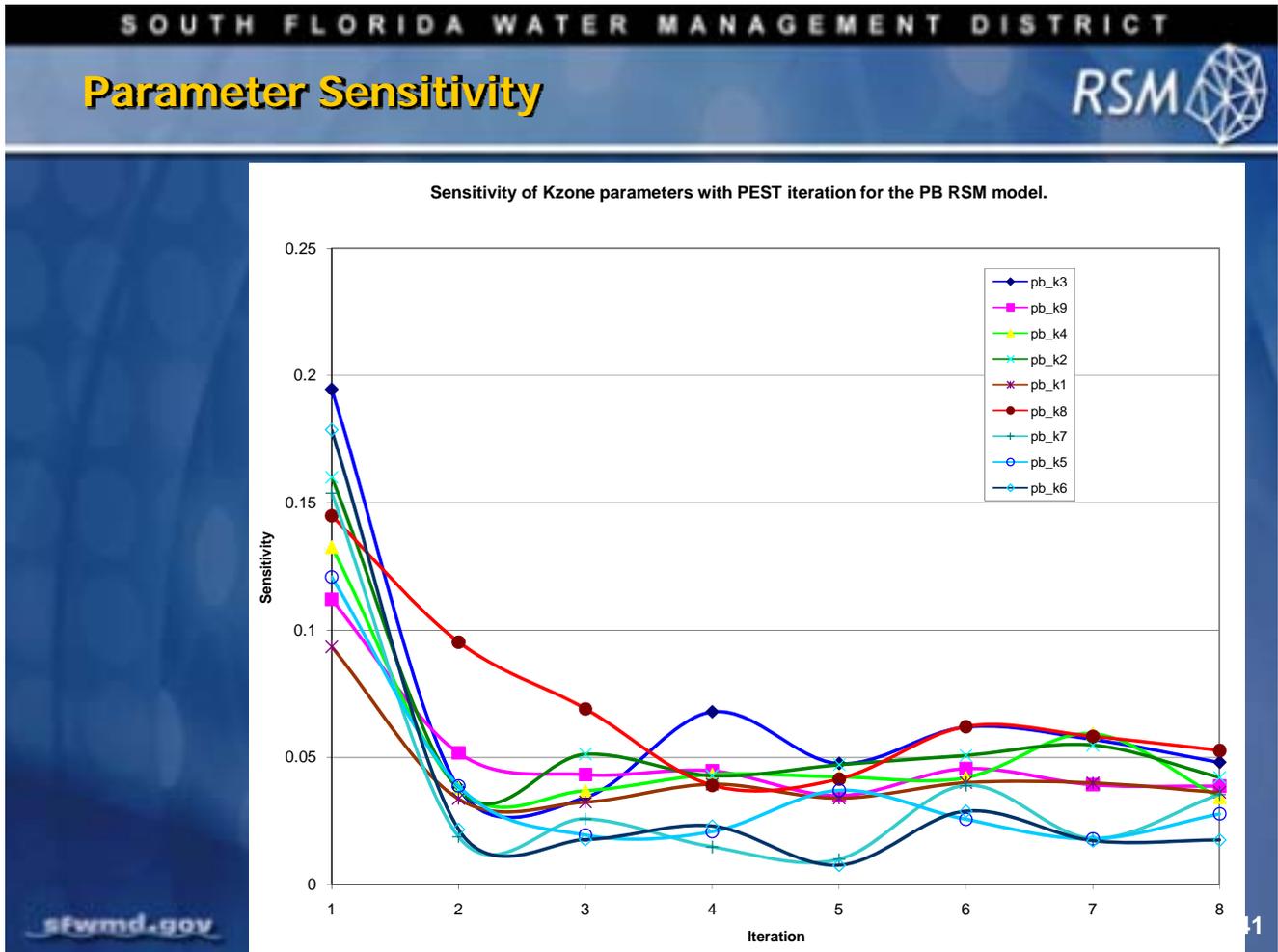
Parameter Sensitivity RSM 

PARAMETER SENSITIVITIES: CASE palm_24

Parameter name	Group	Current value	Sensitivity	Rel. Sensitivity
pb_k1	pb_k	5.681893E-06	9.332172E-02	0.489520
pb_k2	pb_k	1.723028E-04	0.160062	0.602428
pb_k3	pb_k	2.470567E-05	0.194514	0.896167
pb_k4	pb_k	4.550478E-05	0.132597	0.575729
pb_k5	pb_k	4.288966E-05	0.120785	0.527885
pb_k6	pb_k	3.502391E-06	0.178510	0.373883
pb_k7	pb_k	1.576012E-05	0.153908	0.739136
pb_k8	pb_k	4.596347E-05	0.144945	0.629263
pb_k9	pb_k	3.105612E-06	0.111984	0.616790
pb_canal_n2	pb_canal_n	0.100000	0.416621	4.166209E-02
pb_canal_n3	pb_canal_n	3.394257E-02	2.88965	9.808198E-02
pb_canal_kd1	pb_canal_kd	1.000000E-03	0.163237	0.489711
pb_canal_kd2	pb_canal_kd	5.397185E-08	8.217150E-02	0.597209
pb_canal_kd3	pb_canal_kd	6.944105E-06	9.881301E-02	0.509715
pb_canal_kd4	pb_canal_kd	1.000000E-03	0.189590	0.568771
pb_canal_kd5	pb_canal_kd	1.851474E-04	0.169912	0.634195
pb_canal_kd6	pb_canal_kd	8.007235E-06	5.778046E-02	0.294479
pb_canal_kd7	pb_canal_kd	8.617219E-04	0.149150	0.450961
pb_canal_kd8	pb_canal_kd	2.844275E-04	0.163532	0.379887
pb_l8_kmd	pb_lew_kmd	5.187334E-05	9.603935E-02	0.411534
pb_l40n_kmd	pb_lew_kmd	2.765578E-05	0.264366	1.20503
pb_l40s_kmd	pb_lew_kmd	4.832897E-06	0.169778	0.902505
pbwed_lc1	pbwed_lc	1.322213E-05	0.189375	0.923902
pbwed_lc2	pbwed_lc	1.000000E-03	0.134081	0.402244
pbwed_lc3	pbwed_lc	1.299288E-05	0.148422	0.725235
pbwed_lc4	pbwed_lc	1.000000E-08	9.867027E-02	0.789362

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The higher the number, the more sensitive the parameter is. Exclude parameters at the upper and lower bounds. The upper and lower bounds were defined in the control file.



A plot of sensitivities with PEST iterations shows that the parameters are the most sensitive within the first iteration and sensitivity changes with subsequent iterations.

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Parameter Statistics and Confidence Values RSM

- At the end of the PEST run parameter statistics and 95% confidence intervals are reported.
- High levels of parameter uncertainty:
 - Parameter insensitivity
 - Parameter correlations

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All quantities are only approximate because their calculation is based on linearity assumption which is often not true. Regardless of the approximate nature of this analysis, much can be learned about the model, its parameterization and its appropriateness for a specific application. Depending on the use of the model, parameter uncertainty due to high correlations between parameters may not be a defect. High correlations between parameters are easily recognized from the correlation matrix and the eigenvector eigenvalue

analysis. The test is to use the model for predictive analysis. If the predictions made by the model are of the same type as the measurements used in the calibration process, and if the “stress condition” imposed is no different from that which the model went through during calibration, the effect of parameter correlation on model predictions will not be very large.

Parameter uncertainty caused by parameter insensitivity is often more of a challenge than correlation.

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Parameter Confidence Limits RSM

Parameter	Estimated value	Lower 95% limit	Upper 95% limit
pb_k1	5.42E-06	1.98E-06	1.48E-05
pb_k2	2.02E-04	3.13E-05	1.31E-03
pb_k6	3.06E-06	8.58E-10	1.09E-02
pb_k7	1.87E-05	2.07E-10	1.69059
pb_k8	5.40E-05	1.60E-07	1.82E-02
pb_k9	3.59E-06	9.49E-07	1.36E-05
pb_canal_n2	0.1	-0.135347	0.335347
pb_canal_n3	1.00E-02	-1.48E-02	3.48E-02
pb_canal_kd4	1.00E-03	4.65E-05	2.15E-02
pb_canal_kd5	1.87E-04	5.44E-10	64.0926
pb_canal_kd6	8.81E-06	3.29E-08	2.36E-03
pb_canal_kd7	7.93E-04	1.20E-11	52433.7
pb_canal_kd8	2.22E-04	4.03E-11	1219.34
pb_l8_kmd	5.41E-05	2.63E-12	1112.01
pb_l40n_kmd	2.52E-05	2.05E-11	30.9524
pb_l40s_kmd	4.19E-06	3.20E-14	548.779

3

Confidence values provide a useful means of comparing the certainty with which different parameter values are estimated by PEST. Parameters with tight confidence limits are generally not correlated with other parameters. For the Palm Beach County Model the parameters pb_k7, pb_canal_n2, pb_canal_kd5, pb_canal_kd7, pb_canal_kd8 and the levee seepage parameters have large margins of uncertainty.

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PEST Results: Groundwater wells					RSM 
GW Stage Monitoring Site	SFRSM 1984-1995		SFWMM 1984-1995		Criterion Met?
	Bias	RMSE	Bias	RMSE	
BOYNTON_WELL1	-0.61	0.83	n/a	n/a	yes
BOYNTON_WELL2	-0.64	0.72	n/a	n/a	yes
BOYNTON_WELL3	-0.40	0.66	n/a	n/a	yes
PB445	-0.40	0.81	0.01	0.46	yes
PB561	-0.19	0.82	0.13	0.93	yes
PB683	-0.09	0.55	-0.66	0.93	yes
PB685	0.05	1.11	n/a	n/a	yes (marginally)
PB732	-0.14	0.51	-0.02	0.45	yes
PB99	-0.21	0.61	-0.09	0.66	yes
PB1491	2.65	3.36	1.02	2.37	no
PB1494	-0.73	1.07	0.39	0.75	yes
PB1515	-0.43	0.64	-0.18	0.52	yes
PB1639	-0.40	1.48	-0.21	1.34	no
PB1660	-0.53	1.05	0.97	1.24	yes

These are the results for the calibration statistics; bias and root mean-squared error, for the selected wells for the Palm Beach County RSM implementation and the SFWMM. The RSM produced results that are comparable to the SFWMM.

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PEST Results: Secondary Canal Stage RSM 

Secondary Canal Stage Monitoring	SFRSM 1984-1995		SFMMM 1984-1995		Criterion met?
	Bias	RMSE	Bias	RMSE	
Site in WCD					
WCD13.0	-0.12	0.43	n/a	n/a	yes
WCD16.0	0.17	0.46	n/a	n/a	yes
WCD8.5	-0.17	0.48	n/a	n/a	yes
WCD9.3	-0.47	0.68	n/a	n/a	yes

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PEST results for secondary canal stage monitoring locations within the WCDs for the time period 1984-1995. The RSM was able to produce results for canals that are not available in the SFMMM.

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PEST Results: RSM 

Primary canal stage

Primary Canal Stage Monitoring Station	SFRSM 1984-1995		SFMMM 1984-1995		Criterion Met?
	Bias	RMSE	Bias	RMSE	
S5AE-TW	-0.15	0.19	n/a	n/a	yes

Primary canal flow

Primary Canal Flow Monitoring Station	SFRSM 1984-1995		SFMMM 1984-1995		Criterion Met?
	Bias	RMSE	Bias	RMSE	
S155	-3876.96	10218.30	-3214.81	8131.51	yes

Cumulative Demand (cfs-days)

WCD Flow Monitoring Site	SFRSM 1984-1995		SFMMM 1984-1995		Criterion Met?
	Bias	RMSE	Bias	RMSE	
SUMFLOW-WCD16.0	3885.03	5071.46	n/a	n/a	yes (marginally)

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There is only one primary canal in this model, the C51 canal. The stage and canal flow were within acceptable ranges. The negative bias indicates that the calibrated model does not predict the peak flows well. The flow in the secondary system is calibrated against the water supply demands of the WCD. The high bias may be caused by the limited model formulation for the WCD and the poor quality data available for calibration.

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Palm Beach County RSM Calibration-Summary



- For groundwater levels or surface water stages the calibration was satisfactory if either criterion was met:
 - absolute criterion (within ± 1.0 foot) or
 - relative criterion (as good as SFWMM calibration)
- For flows, the criterion was that the measured and computed monthly flow volumes need to be of the same direction and order of magnitude.
- After 22 PEST calibration runs all the calibration criteria were met.

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The automated parameter estimation software PEST was used for the Palm Beach model calibration given the complexities of the model and the large number of model parameters and observation data involved. PEST analysis was conducted by creating parameter zones for aquifer conductivity, the canal network leakance and Manning's n , the lumped leakance for WCD canals, the levee seepage coefficients and the conductance for the tidal boundaries. Objective was to minimize the weighted sum of squares of the bias and RMSE calculated at each observation point.

KNOWLEDGE ASSESSMENT

(pre- and post-lecture quiz to assess efficacy of training materials)

1. What are the two common components of objective functions used for calibrating RSM?
2. How are spatially distributed parameters implemented in RSM?
3. Which parameters are implemented in zones?
4. What are three primary files need to run PEST?
5. Within the PEST control file, what values are provided with each model parameter?
6. What values are provided with each observation?
7. What information is provided in the template files?
8. What processes are implemented in the *run_it.sh* script?
9. What information is in the *fetch_calib.ctl* file?
10. How do we view phi values and what do they tell us about the PEST run?
11. Why do we want to review the parameter correlation coefficients?
12. What do the eigenvectors tell us about the model parameters?
13. What does the condition number tell us?
14. Which are parameter sensitivities important to review?

Answers

1. Bias and root mean squared error (RMSE).
2. The spatially distributed parameters are lumped together into “zones” of equal value.
3. Hydraulic conductivity, canal leakance, manning’s n, canal conductance, levee seepage and tidal general head boundary conditions.
4. Control file, template file and instruction file.
5. The current value, lower limit and upper limit for parameter adjustment are provide for each parameter.
6. The initial value and weight for including in the objective function.
7. The template files contain placeholders for parameters adjusted during calibration.
8. The run_it.sh script creates the et_kc template file, runs the RSM model and then runs a script that calculates the bias and RMSE values for selected stations used by PEST.
9. The fetch_calib.ctl file identifies the times series DSS files and records that are used by the calcStats.py program to calculate bias and RMSE.
10. The phi values can be extracted from the .rec file using the “grep” command. Phi should decrease with each iteration or the PEST process is not improving the parameter values.
11. The parameter correlation coefficients tell us which parameters are highly correlated and side-tracking the PEST solution.
12. High values for parameters within the eigenvectors identify insensitive parameters.
13. The condition number tells how well posed the calibration problem is. If the value is greater than 10^7 PEST may not be able to solve the problem.
14. Insensitive parameters inhibit the PEST process.



Lab 14: RSM Calibration using PEST

Time Estimate: 2.5 hours

Training Objective: To investigate the use of PEST for calibrating the RSM.

The **Regional Simulation Model (RSM)** can be calibrated using **Parameter Estimation (PEST)** on a simple laptop or desktop Linux computer. However, typically the calibration is conducted on an 80-node Linux cluster using the **parallel PEST (PPEST)** methods.

This lab reviews the results of a complete PEST calibration and implements a PEST calibration on the **Biscayne Bay Coastal Wetlands (BBCW) RSM** with five variables.

This is a simple exercise so that the student becomes familiar with the PEST implementation. For more details, see the PEST Manual located in the **labs/lab13_PEST** directory.

**NOTE:**

For ease of navigation, you may wish to set an environment variable to the directory where you install the RSM code using the syntax

```
setenv RSM <path>
```

For SFWMD modelers, the path you should use for the NAS is:

```
/nw/oomdata_ws/nw/oom/sfrsm/workdirs/<username>/trunk
```

```
setenv RSM
```

```
/nw/oomdata_ws/nw/oom/sfrsm/workdirs/<username>/trunk
```

Once you have set the RSM environment variable to your trunk path, you can use \$RSM in any path statement, such as:

```
cd $RSM/benchmarks
```

Training files are currently located in the following directories:

```
INTERNAL_TRAINING
|
|__data
|   |__geographic
|   |__C111
|   |__rain+et
|   |__glades_lecsa
|   |__losa_eaa
|   |__BBCW
|
|__trunk
|   |__benchmarks
|   |__hpmbud
|
|__labs
```

Files for this lab are located in the labs/lab14_RSM_PEST directory. Additional materials in the directory include:

PEST User Manual (**pestman.pdf**)

BBCW7.ppt

BBCW_13_Run_Report_021407.doc

PEST_addendum_11.pdf

Activity 14.1 Reviewing PEST Results for Biscayne Bay Coastal Wetlands RSM

Overview

Activity 14.1 includes two exercises:

- **Exercise 14.1.1.** Review results of BBCW PEST run
- **Exercise 14.1.2.** Create statistics for BBCW PEST run

This activity is designed to review the files associated with a PEST run. Several PEST runs were conducted for the Biscayne Bay Coastal Wetlands (BBCW) and examining the directory content is useful to determine how the PEST runs were set up and to analyze the outcomes.

Exercise 14.1.1 Reviews results of BBCW PEST run.

1. Go to the BBCW RSM PEST model directory to investigate the results of the PEST calibration: `$RSM/data/BBCW/Final_Results_BBW16_sens1`
2. Find the PEST files and information to answer the following questions:
 - How many parameters are being estimated?
 - How many parameter groups are used?
 - What are the groups?
 - In what input files are the parameters located?
 - How many observations are used for calibration?
 - What kinds of data are used for calibration?
 - How many of each?

HINT



The parameters being calibrated are in the template files (*.tpl)

3. Plot the change in the objective function Phi.
 - How many model runs were made?
 - How many iterations were conducted?
 - How many parameters were highly correlated?

HINT



grep the values of "phi" from the *.rec file.
(`grep -n phi bbw16.rec`)

4. Plot the **correlation coefficients** using the RSM **Graphical User Interface (RSM GUI)** tools.

HINT



See Lecture 6 for use of RSM GUI.

5. Which observations are important to the calibration?
 - Run “**Identpar**” utility for PEST where 8 is the number of singular values to use:
identpar bbw_16.pst 8 outbase outfile.dat identfile.dat
 - Import **identfile.dat** into Excel, transpose the values and plot a stacked bar chart of the observation with the **eigenvectors**.

Exercise 14.1.2 Create statistics for the PEST model run.

Look at the results from the PEST run. After obtaining the results from PEST, the model was rerun with standard output: flowgages, global monitors and water budgets. These data are useful for developing an understanding of the hydrology of the system.

Although the performance measures are constructed from model metrics, these cannot be run with PEST because the resulting netCDF file is too large and the model would take too long to run.

The post-processing from the RSM calibration runs produces goodness-of-fit statistics between simulated values and observed data (canal and groundwater stages, and canal flows) and results from the **South Florida Water Management Model (SFWMM)**. We can also compare the calibration statistics of the SFWMM simulations with the historical data.

The statistics can be created using the command line **jython (Java/Python)** script or through the **RSM GUI**. There are two commands for calculating the statistics: **calcStats.py** that calculates the bias and **Root Mean-Squared Error (RMSE)** for stage and flow time series, and **makePlots.py** that creates the time series plots for comparing runs.

1. Go to the `$RSM/data/BBCW/Final_Results_BBW16_sens1` directory.
2. Run **calcStats.py**. (The file `bbcw_fetch_94-00.ct1` (Fig. 14.1) contains the identification of the files and the time series to be used in the comparison.)

```
/opt/local/share2/bin/dssvue ../bin/calcStats_94-00.py ../bin/bbw_fetch_94-00.ct1
```

3. Create time series plots for the RSM PEST run.

Time series plots can be created using a command line script or through the **RSM GUI**. Plots can be made of the RSM simulated heads plotted against historical data and the SFWMM simulated data for the same time period.

Run **makePlots_94-00.py** in the `./BBCW/Final_Results_BBW16_sens1/plots94-00` directory.

```
/opt/local/share2/bin/dssvue ../bin/makePlots_94-00.py ../bbcw_fetch_94-00_for_plots.ct1
```

4. Observe the results in this subdirectory.
 - At which sites did the RSM produce better results than the SFWMM for this set of parameter values?

```

mon SF_S176 /SFRSM/S176/FLOW//1DAY/COMPUTED/ /SFMM/S176/FLOW//1DAY/HISTORICAL/ /SFMM/S176/FLOW//1DAY/SIMULATED/
mon SF_S177 /SFRSM/S177/FLOW//1DAY/COMPUTED/ /SFMM/S177/FLOW//1DAY/HISTORICAL/ /SFMM/S177/FLOW//1DAY/SIMULATED/
mon SF_S178 /SFRSM/S178/FLOW//1DAY/COMPUTED/ /SFMM/S178/FLOW//1DAY/DBHYDRO/ /SFMM/S178/FLOW//1DAY/SIMULATED/
mon SF_S194 /SFRSM/S194/FLOW//1DAY/COMPUTED/ /SFMM/S194/FLOW//1DAY/HISTORICAL/ /SFMM/S194/FLOW//1DAY/SIMULATED/
mon SF_S196 /SFRSM/S196/FLOW//1DAY/COMPUTED/ /SFMM/S196/FLOW//1DAY/HISTORICAL/ /SFMM/S196/FLOW//1DAY/SIMULATED/
mon SF_S165 /SFRSM/S165/FLOW//1DAY/COMPUTED/ /SFMM/S165/FLOW//1DAY/HISTORICAL/ /SFMM/S165/FLOW//1DAY/SIMULATED/

run SH_S118_T /SFRSM/S118_T/STAGE//1DAY/COMPUTED/ /SFMM/S118_T/STAGE//1DAY/HISTORICAL/ /SFMM/S118_T/STAGE//1DAY/SIMULATED/
run SH_S119_T /SFRSM/S119_T/STAGE//1DAY/COMPUTED/ /SFMM/S119_T/STAGE//1DAY/HIST_MOD1/ /SFMM/S119_T/STAGE//1DAY/SIMULATED/
run SH_S121_T /SFRSM/S121_T/STAGE//1DAY/COMPUTED/ /SFMM/S121_T/STAGE//1DAY/HIST_MOD1/ /SFMM/S121_T/STAGE//1DAY/SIMULATED/
run SH_S148_T /SFRSM/S148_T/STAGE//1DAY/COMPUTED/ /SFMM/S148_T/STAGE//1DAY/HIST_MOD1/ /SFMM/S148_T/STAGE//1DAY/SIMULATED/
run SH_S165_T /SFRSM/S165_T/STAGE//1DAY/COMPUTED/ /SFMM/S165_T/STAGE//1DAY/HIST_MOD1/ /SFMM/S165_T/STAGE//1DAY/SIMULATED/
run SH_S166_T /SFRSM/S166_T/STAGE//1DAY/COMPUTED/ /C103/S166_T/STAGE//1DAY/DBHYDRO/ /SFMM/S166_T/STAGE//1DAY/SIMULATED/
run SH_S167_T /SFRSM/S167_T/STAGE//1DAY/COMPUTED/ /SFMM/S167_T/STAGE//1DAY/HIST_MOD1/ /SFMM/S167_T/STAGE//1DAY/SIMULATED/

run CH_EP9R /SFRSM/EP9R/STAGE//1DAY/COMPUTED/ /SFMM/EP9R/STAGE//1DAY/HIST_MOD1/ /SFMM/EP9R/STAGE//1DAY/SIMULATED/
run CH_EP12R /SFRSM/EP12R/STAGE//1DAY/COMPUTED/ /SFMM/EP12R/STAGE//1DAY/HIST_MOD1/ /SFMM/EP12R/STAGE//1DAY/SIMULATED/
run CH_EPSW /SFRSM/EPSW/STAGE//1DAY/COMPUTED/ /SFMM/EPSW/STAGE//1DAY/HIST_MOD1/ /SFMM/EPSW/STAGE//1DAY/SIMULATED/
run CH_EVER1 /SFRSM/EVER1/STAGE//1DAY/COMPUTED/ /SFMM/EVER1/STAGE//1DAY/HIST_MOD1/ /SFMM/EVER1/STAGE//1DAY/SIMULATED/
run CH_EVER2B /SFRSM/EVER2B/STAGE//1DAY/COMPUTED/ /SFMM/EVER2B/STAGE//1DAY/HIST_MOD1/ /SFMM/EVER2B/STAGE//1DAY/SIMULATED/
run CH_EVER3 /SFRSM/EVER3/STAGE//1DAY/COMPUTED/ /SFMM/EVER3/STAGE//1DAY/HIST_MOD1/ /SFMM/EVER3/STAGE//1DAY/SIMULATED/
run CH_EVER4 /SFRSM/EVER4/STAGE//1DAY/COMPUTED/ /SFMM/EVER4/STAGE//1DAY/HIST_MOD1/ /SFMM/EVER4/STAGE//1DAY/SIMULATED/
run CH_F358 /SFRSM/F358/STAGE//1DAY/COMPUTED/ /SFMM/F358/STAGE//1DAY/HIST_MOD1/ /SFMM/F358/STAGE//1DAY/SIMULATED/
run CH_G1183 /SFRSM/G1183/STAGE//1DAY/COMPUTED/ /SFMM/G1183/STAGE//1DAY/HIST_MOD1/ /SFMM/G1183/STAGE//1DAY/SIMULATED/
run CH_G1362 /SFRSM/G1362/STAGE//1DAY/COMPUTED/ /SFMM/G1362/STAGE//1DAY/HIST_MOD1/ /SFMM/G1362/STAGE//1DAY/SIMULATED/
run CH_G1363 /SFRSM/G1363/STAGE//1DAY/COMPUTED/ /SFMM/G1363/STAGE//1DAY/HIST_MOD1/ /SFMM/G1363/STAGE//1DAY/SIMULATED/
run CH_G1486 /SFRSM/G1486/STAGE//1DAY/COMPUTED/ /SFMM/G1486/STAGE//1DAY/HIST_MOD1/ /SFMM/G1486/STAGE//1DAY/SIMULATED/
run CH_G3354 /SFRSM/G3354/STAGE//1DAY/COMPUTED/ /SFMM/G3354/STAGE//1DAY/HIST_MOD1/ /SFMM/G3354/STAGE//1DAY/SIMULATED/
run CH_G3355 /SFRSM/G3355/STAGE//1DAY/COMPUTED/ /SFMM/G3355/STAGE//1DAY/OBSERVED/ /SFMM/G3355/STAGE//1DAY/SIMULATED/

```

Figure 14.1 Contents of `bbw_fetch_calibqh.crl` control file

In **Figure 14.1**, each line of the control file identifies a RSM model output dataset, the corresponding historical data and the corresponding simulation results from the SFWMM. The calcStats.py script will calculate the bias and RMSE between the RSM simulated results and historical data, as well as between the SFWMM simulated results and historical data. The following chart identifies prefixes used in the code:

Prefix	Definition
SF	Segment Flow
SH	Segment Head
CH	Cell Head

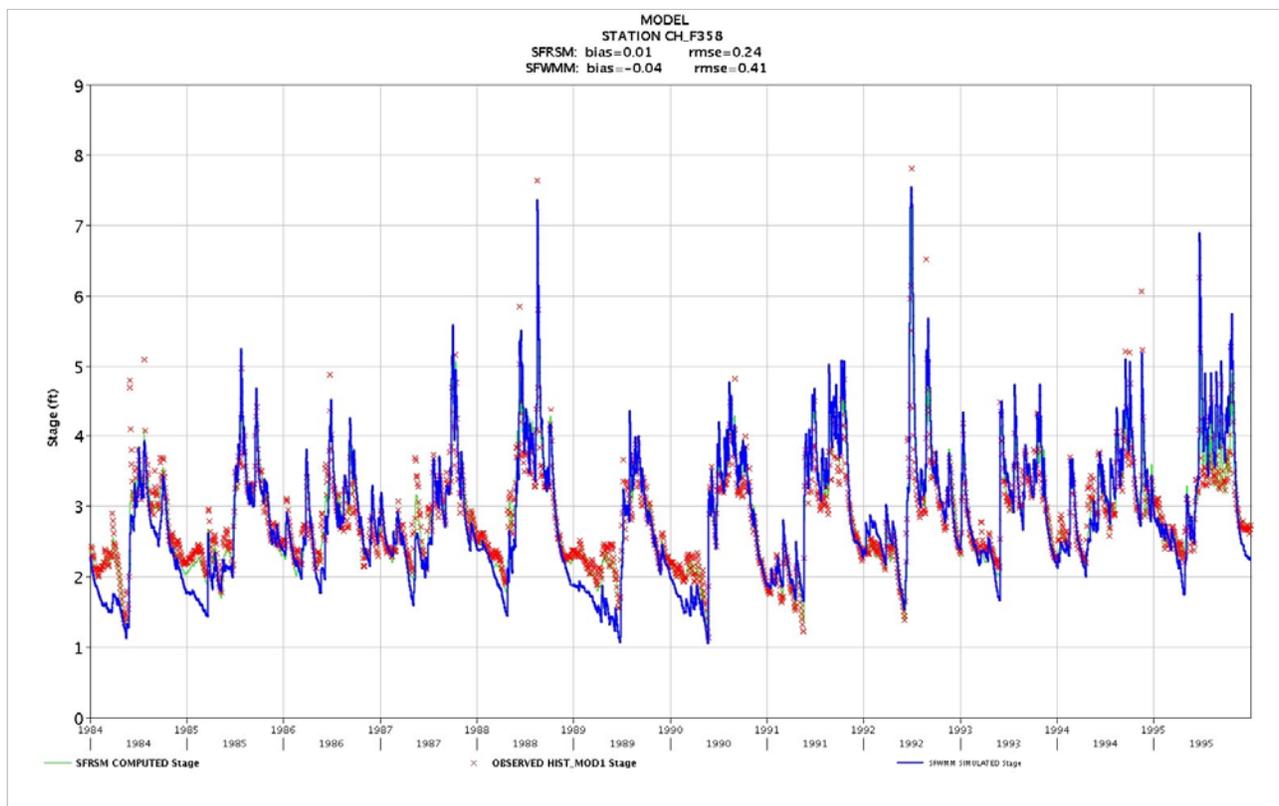


Figure 14.2 Typical time series graph of computed stage, observed historical stage and SFWMM simulated stage created using the makePlots.py python script.

Activity 14.2 Constructing a Simple BBCW RSM PEST run

Overview

Activity 14.2 includes one exercise:

- **Exercise 14.2.1.** Run BBCW PEST using a laptop or a desktop computer

In the next exercise, you will construct a simple PEST run for the **Biscayne Bay Coastal Wetlands (BBCW)**. There are two approaches for completing the PEST run:

- Using a laptop or desktop computer
- Using the South Florida Water Management District (SFWMD) Linux cluster:
dcluster2

The PEST runs are typically run in parallel on the Linux cluster. However, as a training exercise, the Linux cluster is not available.

Exercise 14.2.1 Run BBCW PEST using a laptop or desktop computer

5. Create a new **pest** subdirectory in the **lab14_RSM_PEST/BBCW1** directory:

```
mkdir $RSM/labs/lab14_RSM_PEST/BBCW1/pest
```

6. Copy the following files from the **\$RSM/data/BBCW/pest/** sub-directory into the **BBCW1** directory:

Template file	run_calib_bbcw.xml.tpl
Input files	run_calib_bbcw.xml canal_indexed_attr_122706.xml lvspg_BBCW_12212006.xml tide_wallghb.xml
hse103 files* <small>*this model runs an older version of RSM</small>	hse103 hse103.dtd
Instruction file	residuals.ins
PEST control file	bbcw_qh.pst
output	residuals.out
Batch file	run_it_ef.sh (copy this file from BBCW1 directory into the pest subdirectory for running PEST and post-processing statistics for objective function)

7. Edit `run_it_ef.sh` and change the reference location of `hse103`.
8. Edit the `run_calib_bbcw.xml` and `run_calib_bbcw.xml.tpl` files and change the reference location for the `hse103.dtd`, `rainfall` and `refET` files
9. Copy `/bin` directory to the Lab 14 directory:

```
cp -r $RSM/data/BBCW/pest/bin $RSM/labs/lab14_RSM_PEST/BBCW1
```
10. Copy `/input` directory.

```
cp -r $RSM/data/BBCW/pest/input $RSM/labs/lab14_RSM_PEST/BBCW1
```
11. Make an output directory. Which parameters will be calibrated in this run?

```
mkdir output
```
12. In the `$RSM/labs/lab14_RSM_PEST/BBCW1/bin` directory, check/edit the file `bbcw_fetch_calibqh.ch` to make sure that the references to the input files on the first line are correct.
13. Run the PEST check utility to ensure that the necessary files are okay.

```
pestchek bbcw_qh.pst
```
14. Run PEST from the batch file

```
pest bbcw_qh.pst
```



NOTE:

This PEST run will take approximately 2.5 hours to run on a Dell Latitude D810 laptop with 2MB DDRR memory.

If there is insufficient time to complete the model run, the results can be reviewed by copying the `$RSM/data/BBCW/pest/bbcw_ef*` files and looking at the results.

`bbcw_ef.rec` – model run, correlation coefficients, objective function, etc.

`bbcw_ef.par` – final best fit parameter values

15. Evaluate the PEST results.
 - Plot the **Phi** values and look at the convergence of the PEST calibration.
 - Evaluate the **eigenvectors**: Is the ratio between the highest and lowest less than 10^6 ?

HINT



Look at the eigenvalues at the bottom of the `bbcw_ef.rec` file.

- Are the parameters correlated?

HINT



Look at the `bbcw_ef.rec` or `bbcw_ef.mtt` files.

- How much has the final parameter values changed from the initial values?
- What are the confidence intervals for the parameters?

Answers for Lab 14.

Exercise 14.1.1

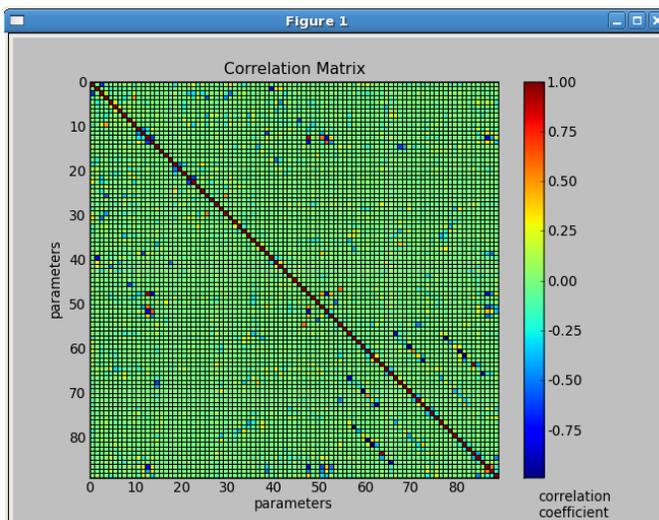
2. PEST answers:

- 95 parameters
- 5 groups
- Parameter groups:
 - hydraulic conductivity
 - levee seepage
 - canal leakage coefficient
 - wcd leakage coefficient
 - general head boundary condition conductivity
- input files for parameters:
 - run_PEST_calib_bbw.xml.tpl
 - BBW_canal_indexed_attr.xml.tpl
 - BBW_levee_seepage.xml.tpl
 - BBW_tide_bc_wall_ghb.xml.tpl,
 - BBW_Northern_BC_Cell_ghb.xml.tpl, BBW_Western_BC_Wall_ghb.xml.tpl ,
bbw_wcd.xml.tpl
- 1042 observations
- CH – cell head (256); SH – segment head (66); SF – monthly segment flow (720)

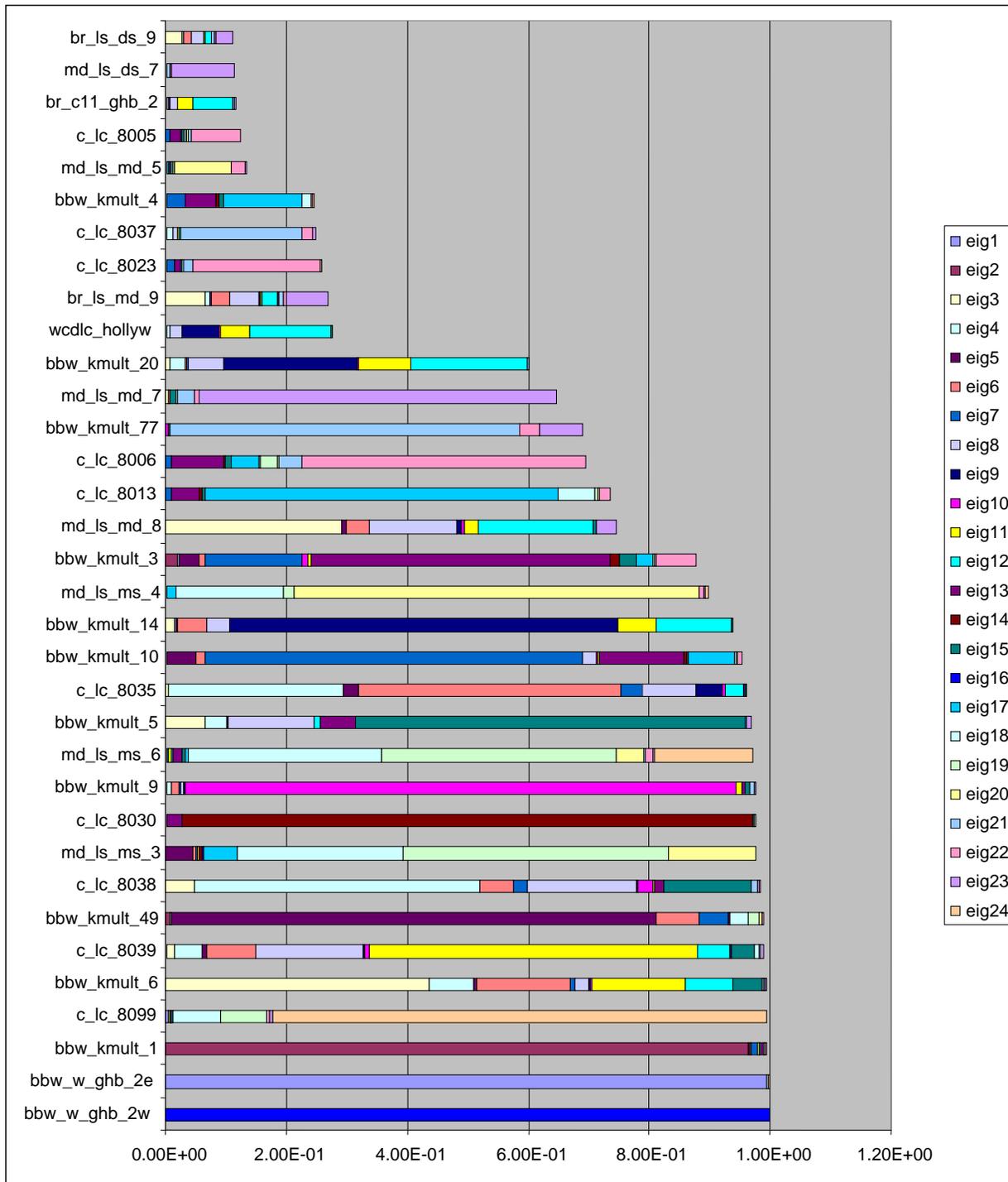
3. See the plot in the PhiPlot.xls file in the Lab14_RSM_PEST directory.

- 1840 model runs
- 16 iterations
- about 23 parameter pairs. Dark blue and dark red in Correlation matrix.

4. Correlation matrix:



5. Important Observations:



Exercise 14.1.2

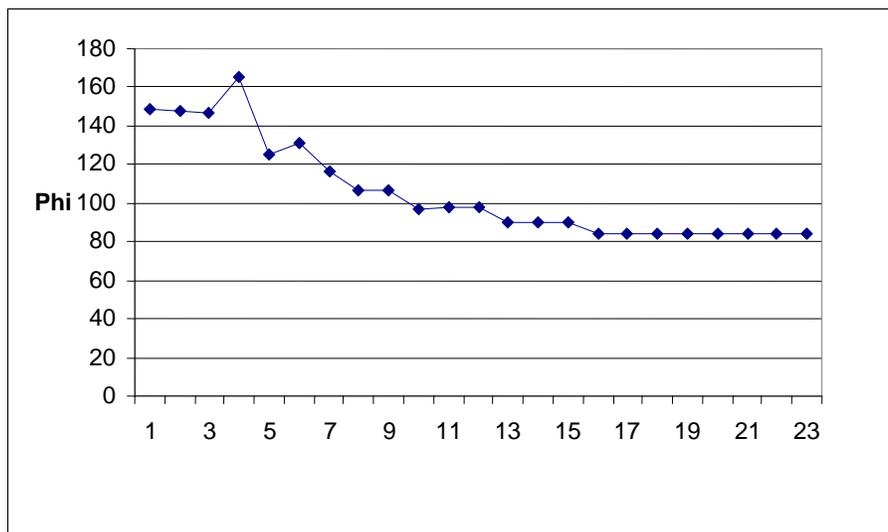
4. Several sites including E146, E158, EPSW, EVER1, EVER2, F358, FROGP, G551, G553.

Exercise 14.2.1

7. Calibrated parameters:

- Kmult_1
- Kmult_3
- Kmult_4
- Kmult_8
- Kmult_10
- Kmult_200
- Transmissivity

11. Simple BBCW RSM PEST calibration

Phi PlotEigenvalues ----->

5.9048E-03 8.2884E-03 1.0089E-02 2.8936E-02 0.1428 0.4133
 Ratio: 70 very well conditioned for this example.

Parameter correlation coefficient matrix ----->

None of the parameters are highly correlated.

	kmult_1	kmult_3	kmult_4	kmult_8	kmult_10	kmult_200
kmult_1	1.000	-0.1860	-0.1565	0.2750	0.0615	0.02722
kmult_3	-0.1860	1.000	0.0106	-0.0905	0.4792	-0.2036
kmult_4	-0.1565	0.0106	1.000	-0.4591	0.3207	-0.1277
kmult_8	0.2750	-0.0905	-0.4591	1.000	-0.2770	0.1036
kmult_10	-0.0601	0.4792	0.3207	-0.2770	1.000	-0.4209
kmult_200	0.0272	-0.2036	-0.1277	0.1036	-0.4209	1.000

Initial versus Final values:

Initial value	Final Estimate
---------------	----------------

kmult_1	2.000000E-04	4.4061738E-05
kmult_3	7.000000E-04	3.4940013E-05
kmult_4	5.000000E-04	4.9057131E-04
kmult_8	2.000000E-05	1.8639147E-05
kmult_10	6.000000E-05	1.3315163E-05
kmult_200	2.000000E-06	2.3148000E-04

Confidence limits:

Parameter	Estimated value	95% percent confidence limits	
		lower limit	upper limit
kmult_1	4.406174E-05	2.928304E-05	6.629902E-05
kmult_3	3.494001E-05	2.107575E-05	5.792460E-05
kmult_4	4.905713E-04	5.676425E-05	4.239644E-03
kmult_8	1.863915E-05	1.431565E-06	2.426840E-04
kmult_10	1.331516E-05	6.530047E-06	2.715043E-05
kmult_200	2.314800E-04	1.415146E-04	3.786394E-04

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